딥러닝 모델 엑기스 추출
Knowledge Distillation

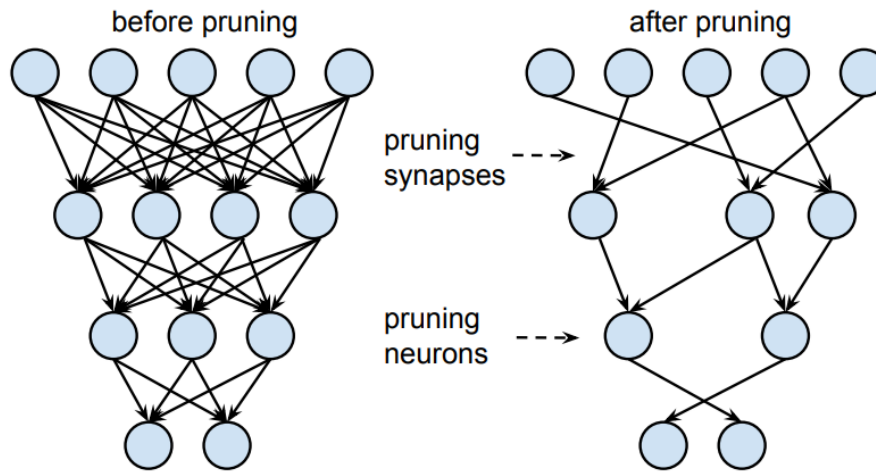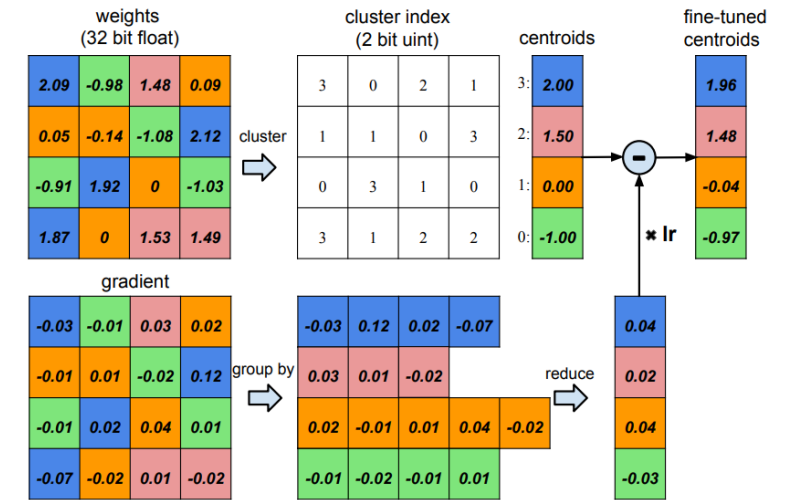**Machine Learning & Visual Computing Lab**
김유민

1

CONTEXT

- Compression Methods
- Distillation
- Papers
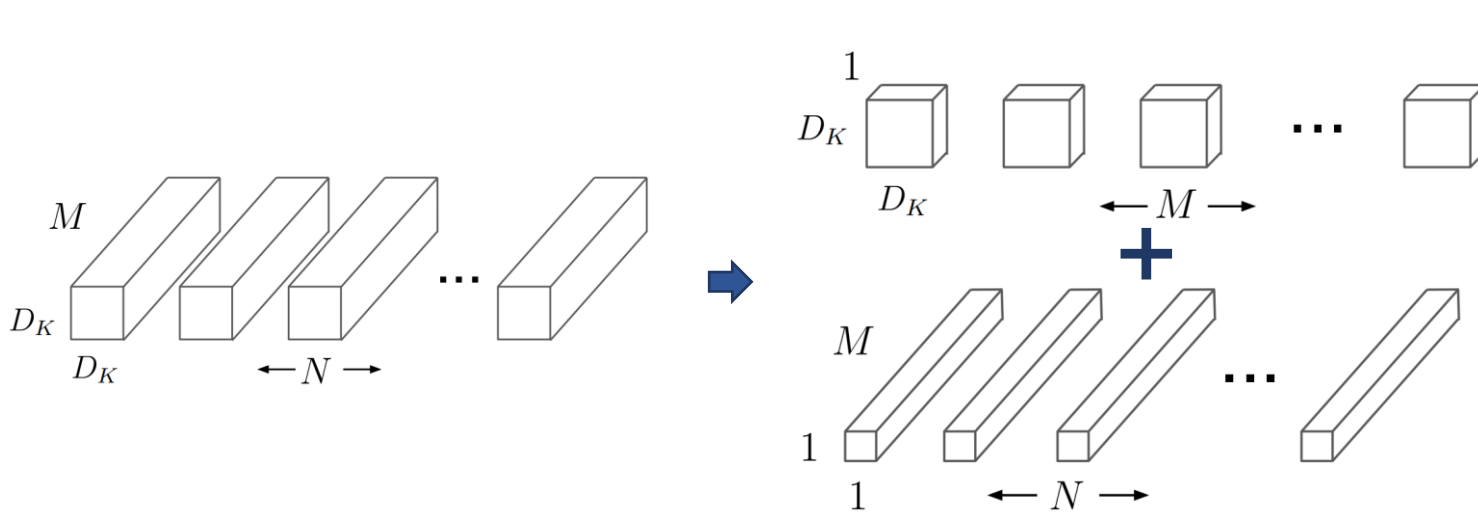- Summary

COMPRESSION METHODS

- Pruning
- Quantization
- Efficient Design
- Distillation
- Etc...

<Weight Pruning[1]>
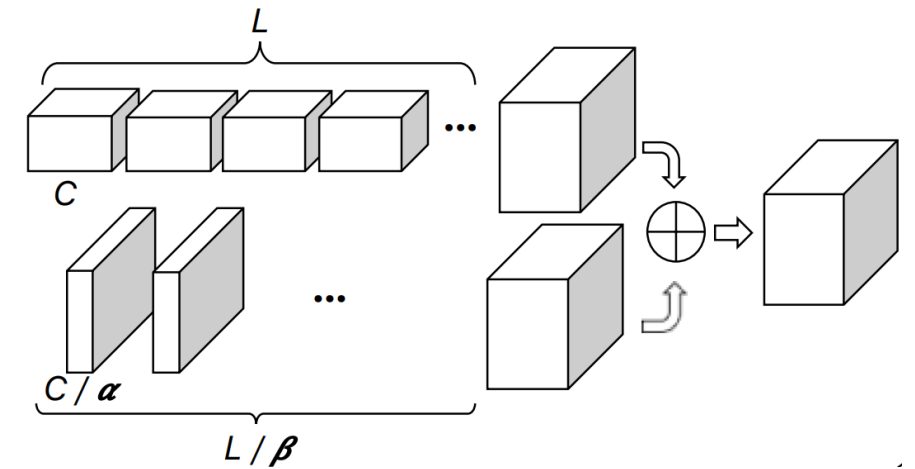
<Weight Quantization[2]>

<Depthwise separable convolution[3]>

<Big-little net architecture[4]>

[1] Song Han, Jeff Pool, John Tran and Willan J. Dally. Learning both Weights and Connections for Efficient Neural Networks. In *NIPS*, 2015.
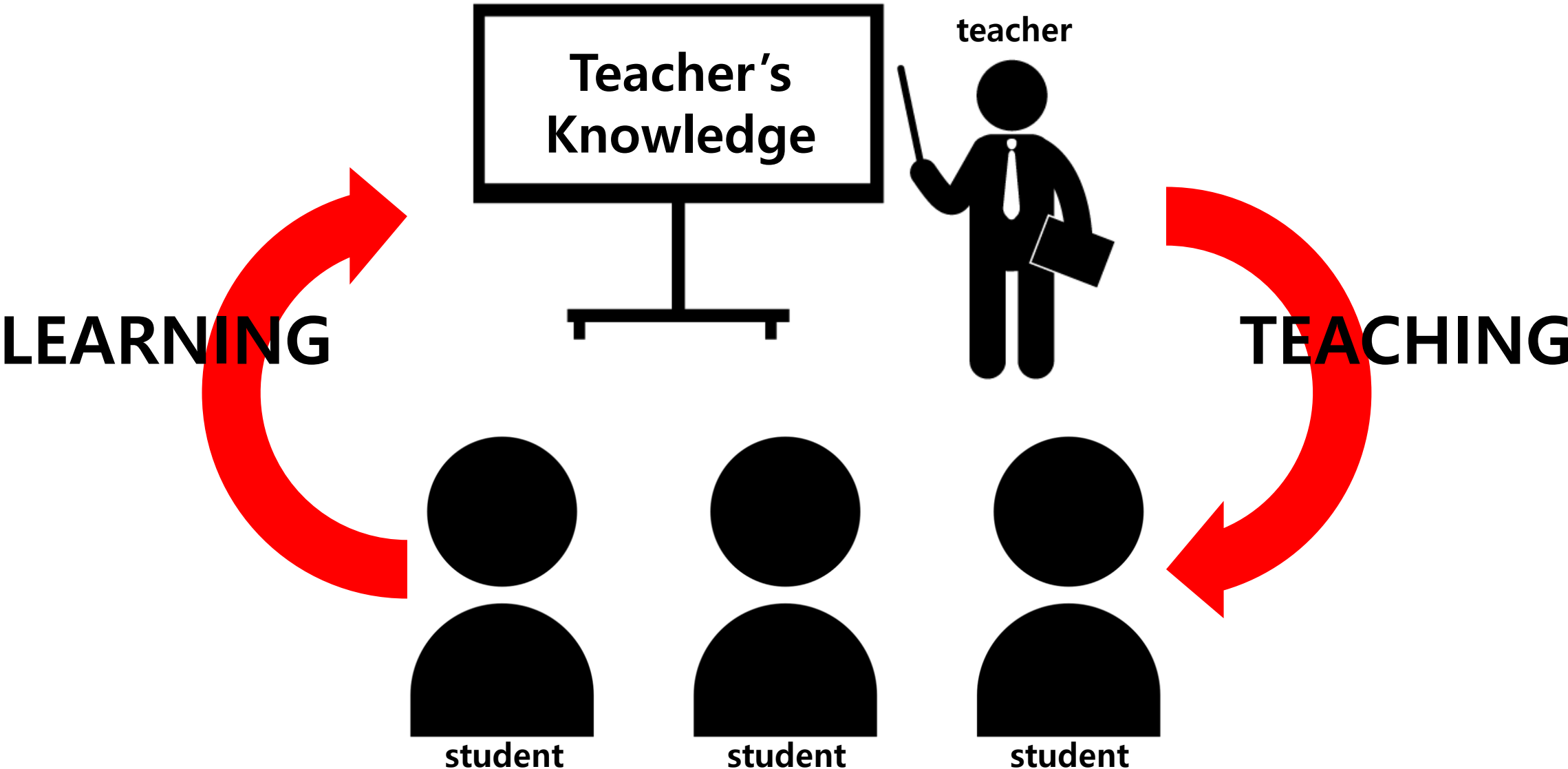
[2] Song Han, Huizi Mao and William J. Dally. Deep Compression: Compressing Deep Neural Networks with Pruning, Trained Quantization and Huffman Coding. In *ICLR*, 2016.

[3] Andrew G. Howard, Menglong Zhu, Bo Chen, Dmitry Kalenichenko, Weijun Wang, Tobias Weyand, Marco Andreetto and Hartwig Adam. MobileNets: Efficient Convolutional Neural Networks for Mobile Vision Applications. In *arXiv*, 2017.
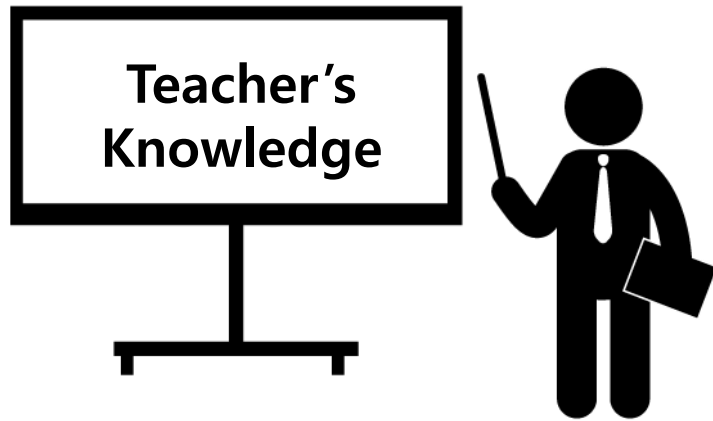
[4] Chun-Fu(Richard) Chen et al. Big-Little Net: an Efficient Multi-Scale Feature Representation for visual and speech recognition. In *ICLR*, 2019.

DISTILLATION

Teacher's Knowledge

teacher

LEARNING

TEACHING

student   **student**   **student**

Teacher–Student Relation in Deep Neural Network

Large Neural Network
Classification Accuracy : 93.33%

<Teacher Network>

teacher

Small Neural Network
Classification Accuracy : 58.34%

<Student Network>

student

Christian Szegedy, Wei Liu, Yangqing Jia, Pierre Sermanet, Scitt Reed, Dragomir Anguelov, Dumitru Erhan, Vincent Vanhoucke and Andrew Rabinovich. Going Deeper with Convolutions. In *CVPR*, 2015.
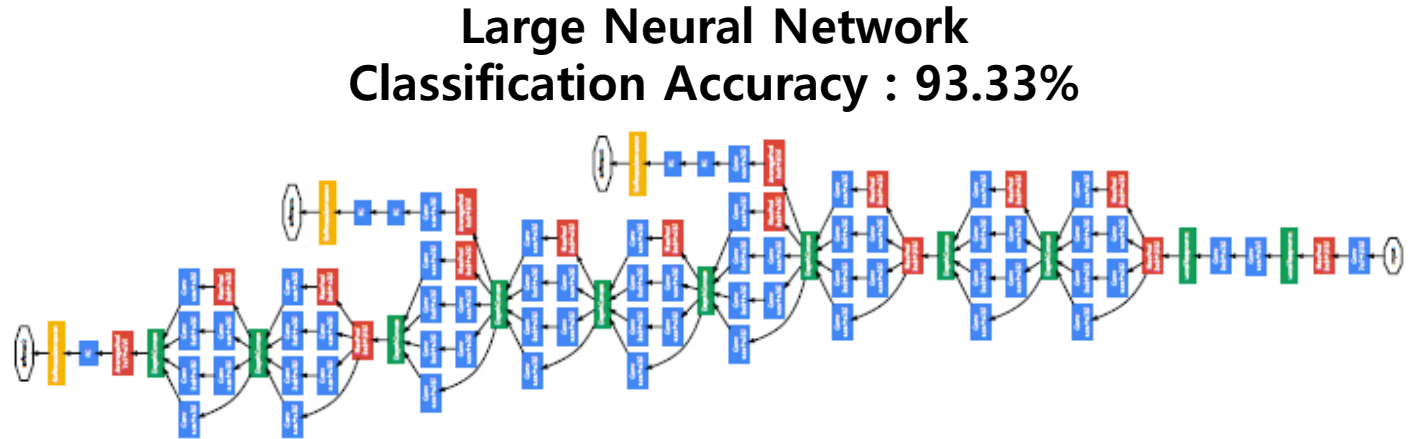
Teacher–Student Relation in Deep Neural Network

Large Neural Network
Classification Accuracy : 93.33%

Teacher's Knowledge

teacher

LEARNING

TEACHING

student

=

<Teacher Network>

LEARNING

TEACHING

Small Neural Network
Classification Accuracy : 58.34%

=

<Student Network>

Christian Szegedy, Wei Liu, Yangqing Jia, Pierre Sermanet, Scitt Reed, Dragomir Anguelov, Dumitru Erhan, Vincent Vanhoucke and Andrew Rabinovich. Going Deeper with Convolutions. In *CVPR*, 2015.

Teacher–Student Relation in Deep Neural Network

Teacher's Knowledge
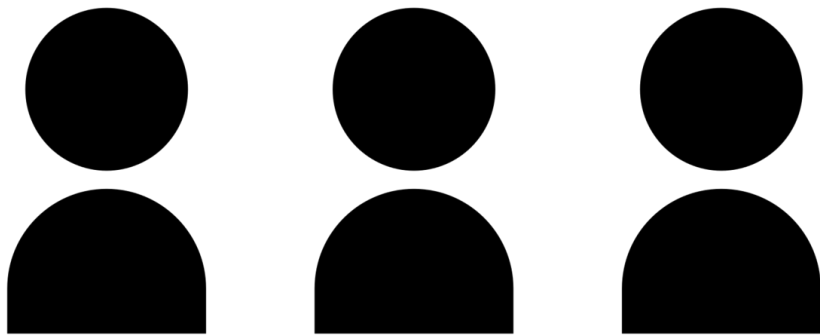
teacher

=
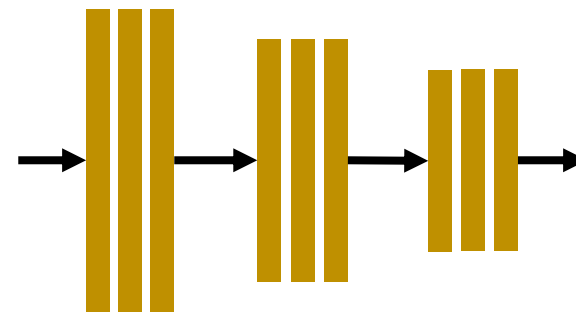
Large Neural Network
Classification Accuracy : 93.33%

<Teacher Network>

student

=

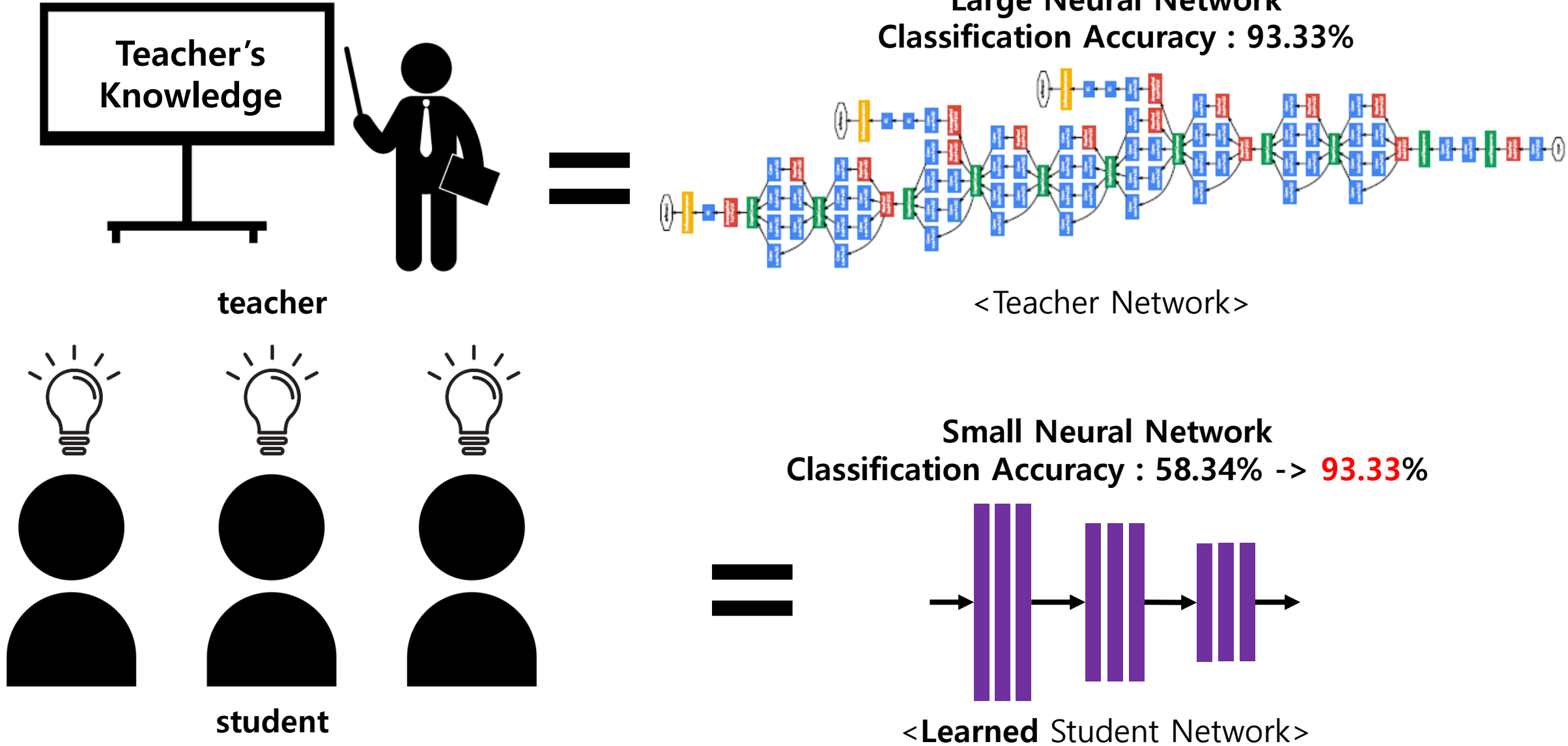**Small Neural Network**
Classification Accuracy : 58.34% -> 93.33%

<**Learned** Student Network>

Christian Szegedy, Wei Liu, Yangqing Jia, Pierre Sermanet, Scitt Reed, Dragomir Anguelov, Dumitru Erhan, Vincent Vanhoucke and Andrew Rabinovich. Going Deeper with Convolutions. In *CVPR*, 2015.
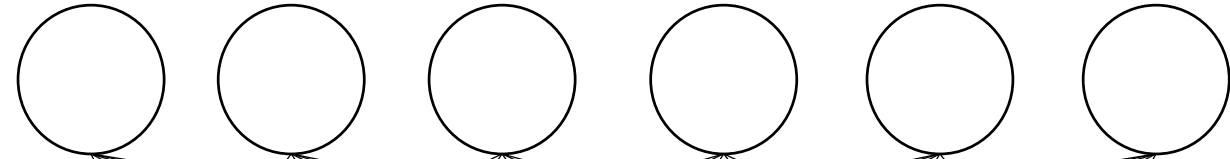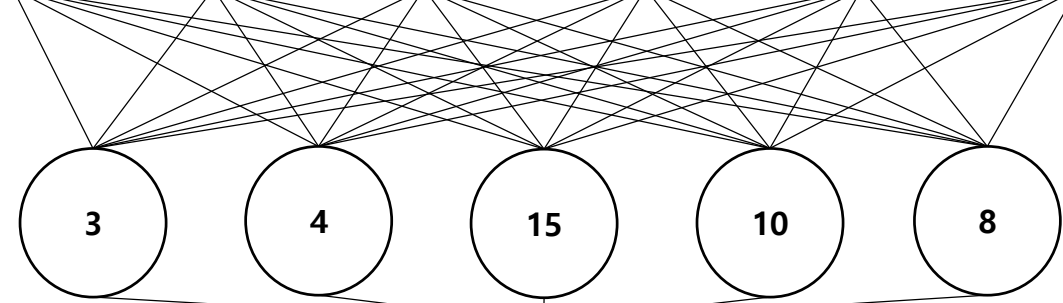
Do Deep Nets Really Need to be Deep?

2014
NIPS

Do Deep Nets Really Need to be Deep?. In *NIPS*, 2014.
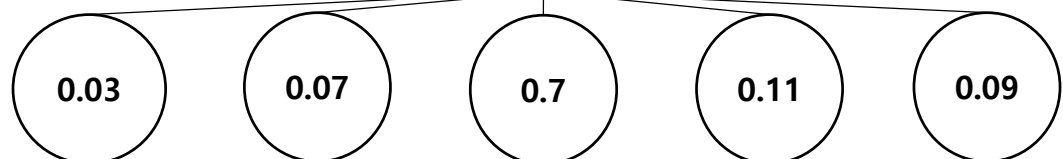
– Lei Jimmy Ba and Rich Caruana.

$n-1_{th}$ **Layer**

n_{th} **Layer(=last layer)**

| 3 | 4 | 15 | 10 | 8 |

$$\text{Softmax}(\widehat{Y}_i = \frac{e^{z_i}}{\sum_{i=1}^{n} e^{z_i}})$$

Final output softmax distribution

| 0.03 | 0.07 | 0.7 | 0.11 | 0.09 |

Cross-entropy Loss : L(Y, $\widehat{Y}$) = -$\sum_i Y_i \log \widehat{Y}$

True label

| 0 | 0 | 1 | 0 | 0 |

Propagation Direction

\<Last section of DNN\>

Animal pictures – www.freepik.com

– Lei Jimmy Ba and Rich Caruana.

$n - 1_{th}$ **Layer** →

n_{th} **Layer(=last layer) => Logits** →
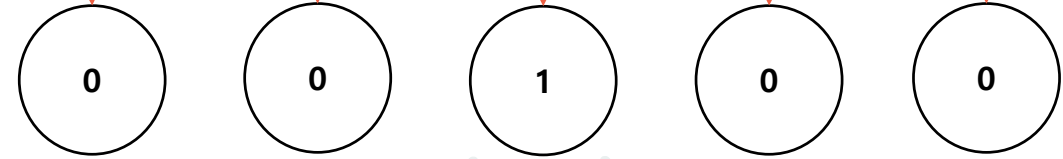
Propagation Direction

$$Softmax(\widehat{Y}_i = \frac{e^{z_i}}{\sum_{i=1}^{n} e^{z_i}})$$

Final output softmax distribution →

Cross-entropy Loss : L($Y, \widehat{Y}$) = -$\sum_i Y_i \log \widehat{Y}$
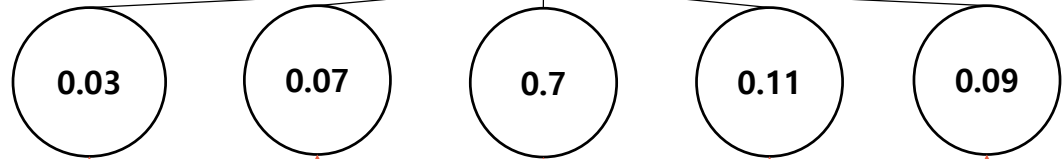
True label →

<Last section of DNN>

Animal pictures – www.freepik.com

Do Deep Nets Really Need to be Deep?. In *NIPS*, 2014.
− Lei Jimmy Ba and Rich Caruana.

Input Image

Teacher Network

Output

Classification Loss

True Label

<1st step. Training Teacher Network>

Animal pictures − www.freepik.com

Do Deep Nets Really Need to be Deep?. In *NIPS*, 2014.

– Lei Jimmy Ba and Rich Caruana.

Freezing all weights(Pre-trained)

Teacher Network

Logit

L2 Loss with each Logits

Logit

Student Network

Classification Loss

<2nd step. Training Student Network>

Cat: 32
Tiger: 24
Dog: 15
Lion: 12
⋮

<Logits>

Cat: 84%
Tiger: 7%
Dog: 3%
Lion: 2%
⋮

<softmax probability>

Animal pictures – www.freepik.com

Do Deep Nets Really Need to be Deep?. In *NIPS*, 2014.

— Lei Jimmy Ba and Rich Caruana.

<Student deosn't overfit>

<Better teacher, Better student>

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Distilling the Knowledge in a Neural Network

Distilling the knowledge in a Neural Network. In *NIPS workshop*, 2014.

– Geoffrey Hinton, Oriol Vinyals and Jeff Dean.

$n - 1_{th}$ **Layer** →

n_{th} **Layer(=last layer) => Logits** →

| 3 | 4 | 15 | 10 | 8 |

$$\text{Softmax}(\widehat{Y}_i = \frac{e^{z_i}}{\sum_{i=1}^{n} e^{z_i}})$$

Final output softmax distribution →

| 0.03 | 0.07 | 0.7 | 0.11 | 0.09 |

Cross-entropy Loss : L($Y, \widehat{Y}$) = $-\sum_i Y_i \log \widehat{Y}$

True label →

| 0 | 0 | 1 | 0 | 0 |

Propagation Direction

<Last section of DNN>

Distilling the knowledge in a Neural Network. In *NIPS workshop*, 2014.

– Geoffrey Hinton, Oriol Vinyals and Jeff Dean.

$n - 1_{th}$ **Layer** →

n_{th} **Layer(=last layer) => Logits** →

Propagation Direction

| 3 | 4 | 15 | 10 | 8 |

$$\text{Softmax}(\widehat{Y}_i = \frac{e^{z_i}}{\sum_{i=1}^{n} e^{z_i}})$$

Final output softmax distribution →

| 0.03 | 0.07 | 0.7 | 0.11 | 0.09 |

Cross-entropy Loss : L($Y, \widehat{Y}$) = -$\sum_i Y_i \log \widehat{Y}$

True label →

| 0 | 0 | 1 | 0 | 0 |

<Last section of DNN>

Distilling the knowledge in a Neural Network. In *NIPS workshop*, 2014.

– Geoffrey Hinton, Oriol Vinyals and Jeff Dean.

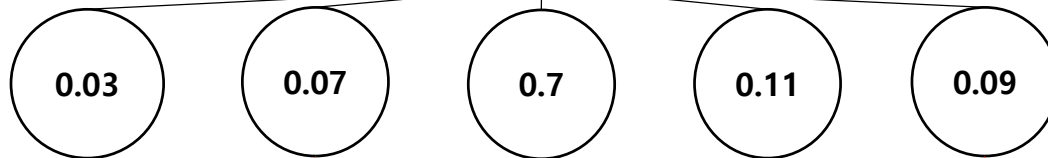$$\widehat{Y_i} = \frac{e^{z_i/T}}{\sum_{i=1}^{n} e^{z_i/T}}$$

<Soft target function>

$$\text{Softmax}(\widehat{Y_i} = \frac{e^{z_i}}{\sum_{i=1}^{n} e^{z_i}})$$

| 3 | 4 | 15 | 10 | 8 |

| 0.03 | 0.07 | 0.7 | 0.11 | 0.09 |

HARD TARGET

| 3 | 4 | 15 | 10 | 8 |

$$\text{Soft Target Function}(\widehat{Y_i} = \frac{e^{z_i/T}}{\sum_{i=1}^{n} e^{z_i/T}})$$

| 0.08 | 0.12 | 0.4 | 0.21 | 0.19 |

SOFT TARGET=> KNOWLEDGE

Probability
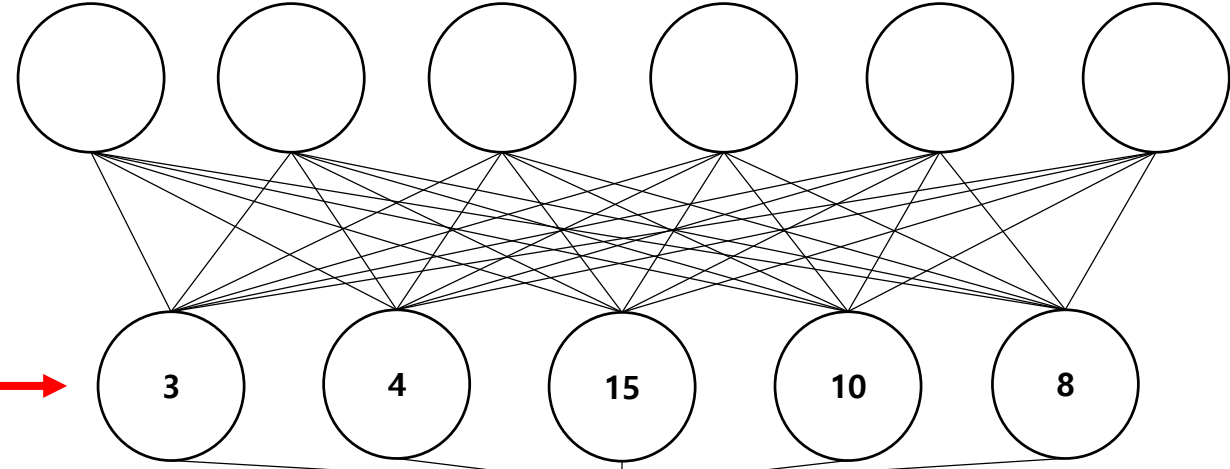
Hard Target

Soft Target

Class index

<Soften the hard target distrubution>

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Distilling the knowledge in a Neural Network. In *NIPS workshop*, 2014.
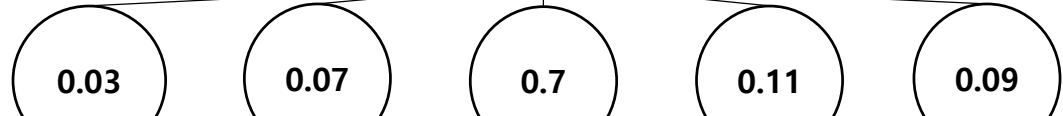– Geoffrey Hinton, Oriol Vinyals and Jeff Dean.

Freezing all weights(Pre-trained)

Teacher Network

Soft Target

Distillation Loss(KL Divergence)

Soft Target

Student Network

Classification Loss

<Knowledge Distillation structure>

Cat: 74%
Tiger: 12%
Dog: 7%
Lion: 2%
⋮

→

Cat: 40%
Tiger: 33%
Dog: 10%
Lion: 5%
⋮

Cat: 2%
Tiger: 84%
Dog: 5%
Lion: 3%
⋮

→

Cat: 7%
Tiger: 50%
Dog: 35%
Lion: 3%
⋮

<Hard target to soft target distribution>

FitNets:
Hints for Thin Deep Nets

FitNets: Hints for Thin Deep Nets. In *ICLR*, 2015.

– Adriana Romero, Nicolas Ballas, Samira Ebrahimi Kahou, Antoine Chassang, Carlo Gatta and Yoshua Bengio.

<1st step. Making thin & deeper student network>

FitNets: Hints for Thin Deep Nets. In *ICLR*, 2015.

– Adriana Romero, Nicolas Ballas, Samira Ebrahimi Kahou, Antoine Chassang, Carlo Gatta and Yoshua Bengio.

$$\mathbf{W}^*_{\mathbf{Guided}} = \underset{\mathbf{W_{Guided}}}{\arg\min} \; \mathcal{L}_{HT}(\mathbf{W_{Guided}}, \mathbf{W_r})$$

W_r

W_{Hint} W_{Guided}

<2nd step. Training through regressor>

<Pre-trained teacher network(Hint)>

Hint   Hint   Hint

$$\mathcal{L}_{HT}(\mathbf{W_{Guided}}, \mathbf{W_r}) = \frac{1}{2}\|u_h(\mathbf{x}; \mathbf{W_{Hint}}) - r(v_g(\mathbf{x}; \mathbf{W_{Guided}}); \mathbf{W_r})\|^2.$$

R   R   R

<Thin & deeper student network(Guided)>

23

FitNets: Hints for Thin Deep Nets. In *ICLR*, 2015.

– Adriana Romero, Nicolas Ballas, Samira Ebrahimi Kahou, Antoine Chassang, Carlo Gatta and Yoshua Bengio.

<Pre-trained teacher network(Hint)>

$$\mathbf{W}_{\mathbf{s}}^{*} = \underset{\mathbf{W_S}}{\operatorname{argmin}} \mathcal{L}_{DK}(\mathbf{W_s})$$

$\mathbf{W_s}$

$\mathbf{W}^{*}_{\textbf{Guided}}$

<3rd step. Training through KD>

$$P_{T}^{\tau} = \operatorname{softmax}\left(\frac{\mathbf{a}_{T}}{\tau}\right)$$

Knowledge Distillation Loss

$$\mathcal{L}_{KD}(\mathbf{W_S}) = \mathcal{H}(\mathbf{y_{true}}, P_S) + \lambda\mathcal{H}(P_T^{\tau}, P_S^{\tau})$$

$$P_{S}^{\tau} = \operatorname{softmax}\left(\frac{\mathbf{a}_{S}}{\tau}\right)$$

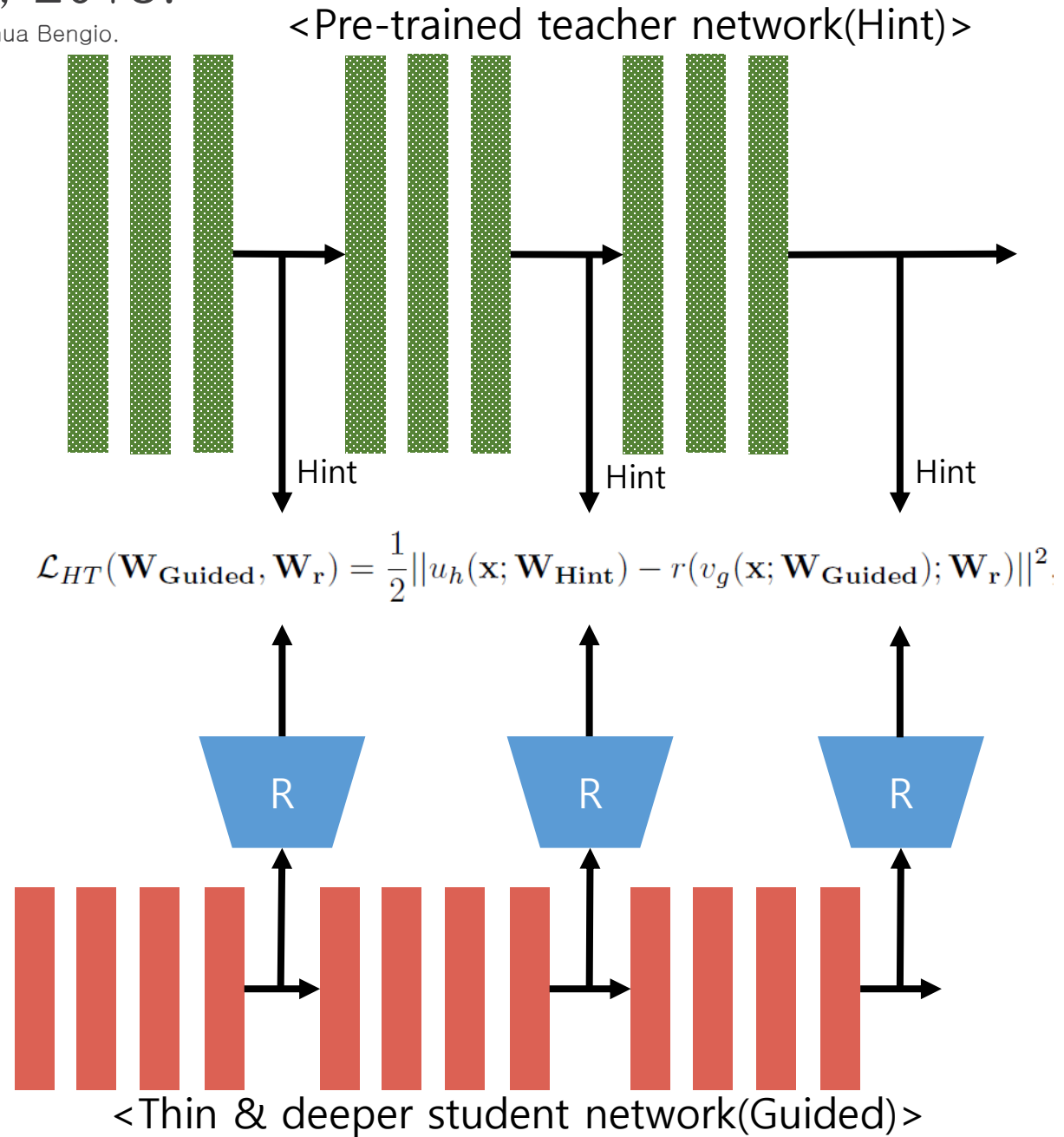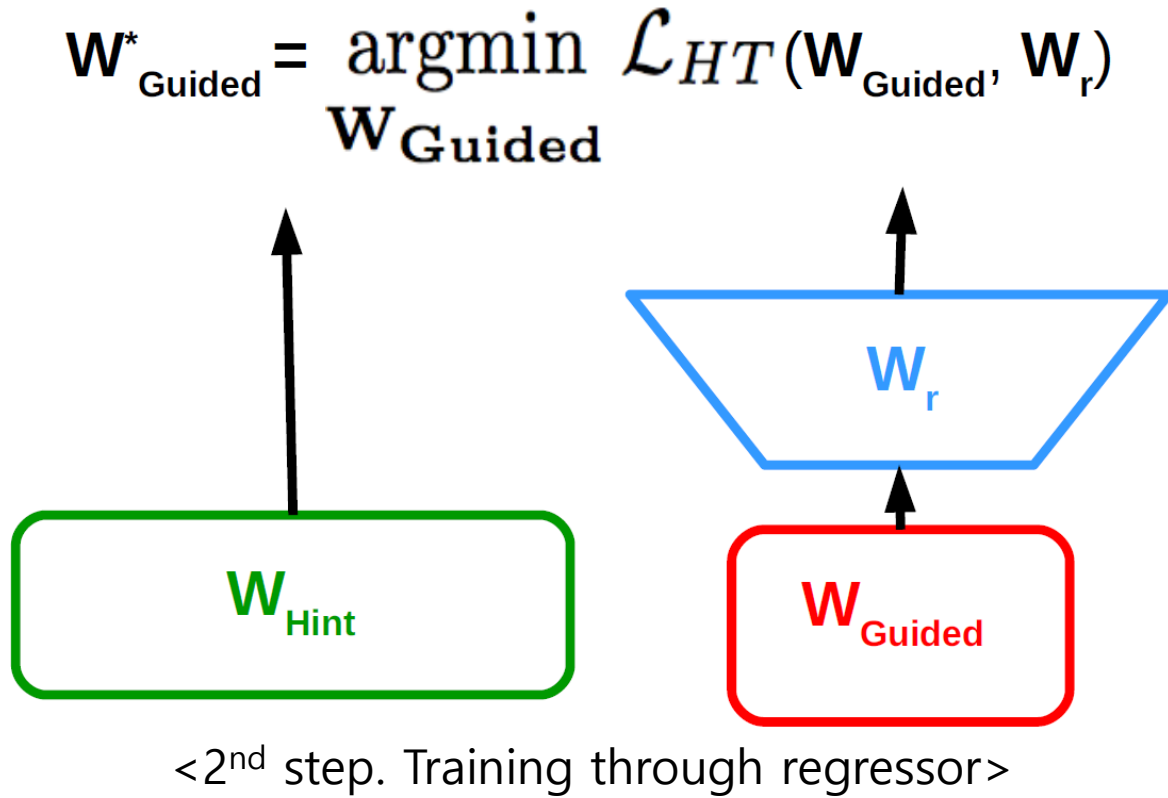<Thin & deeper student network(Guided)>

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FitNets: Hints for Thin Deep Nets. In *ICLR*, 2015.

– Adriana Romero, Nicolas Ballas, Samira Ebrahimi Kahou, Antoine Chassang, Carlo Gatta and Yoshua Bengio.
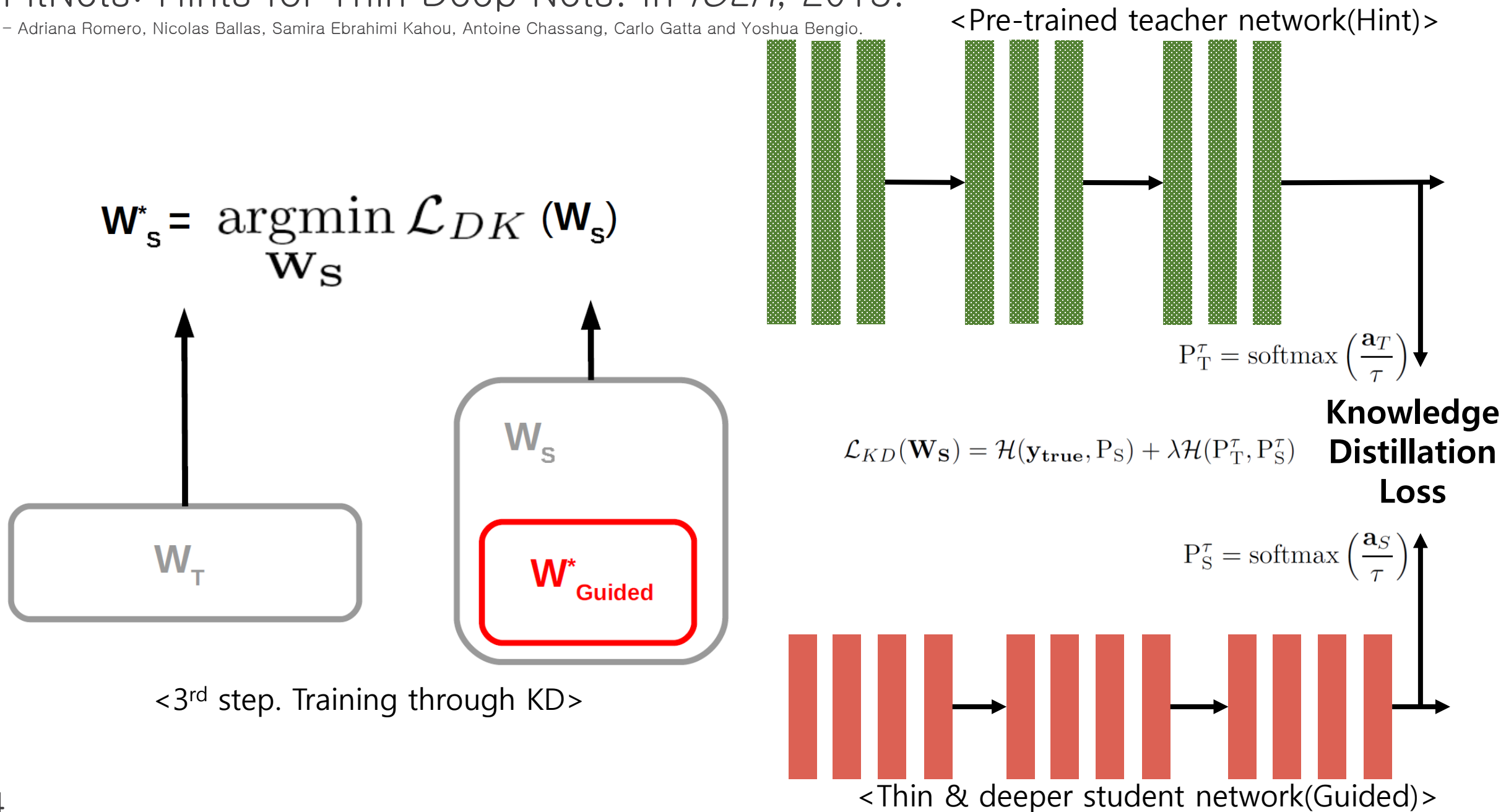
Algorithm	# params	Accuracy
Compression		
FitNet	~2.5M	**64.96%**
Teacher	~9M	63.54%
State-of-the-art methods		
Maxout		61.43%
Network in Network		64.32%
Deeply-Supervised Networks		**65.43%**

Table 2: Accuracy on CIFAR-100

Network	# layers	# params	# mult	Acc	Speed-up	Compression rate
Teacher	5	~9M	~725M	90.18%	1	1
FitNet 1	11	~250K	~30M	89.01%	**13.36**	**36**
FitNet 2	11	~862K	~108M	91.06%	4.64	10.44
FitNet 3	13	~1.6M	~392M	91.10%	1.37	5.62
FitNet 4	19	~2.5M	~382M	**91.61%**	1.52	3.60

Table 5: Accuracy/Speed Trade-off on CIFAR-10.

A Gift from Knowledge Distillation: Fast Optimization, Network Minimization and Transfer Learning

A Gift from Knowledge Distillation: Fast Optimization, Network Minimization and Transfer Learning. In *CVPR*, 2017.

– Junho Yim, Donggyu Joo, Jihoon Bae and Junmo Kim.

FLOW FLOW FLOW

$$\mathbf{G}(\boldsymbol{a_1}, \ldots, \boldsymbol{a_n}) =$$
$$\begin{pmatrix} (\boldsymbol{a_1}, \boldsymbol{a_1}) & (\boldsymbol{a_1}, \boldsymbol{a_2}) & \cdots & (\boldsymbol{a_1}, \boldsymbol{a_n}) \\ (\boldsymbol{a_2}, \boldsymbol{a_1}) & (\boldsymbol{a_2}, \boldsymbol{a_2}) & \cdots & (\boldsymbol{a_2}, \boldsymbol{a_n}) \\ \vdots & \vdots & \ddots & \vdots \\ (\boldsymbol{a_n}, \boldsymbol{a_1}) & (\boldsymbol{a_n}, \boldsymbol{a_2}) & \cdots & (\boldsymbol{a_n}, \boldsymbol{a_n}) \end{pmatrix}$$

<Gram Matrix definition>

* (a, b) = Inner product of a and b

Feature map

Feature map

Teacher Net

Transfer the distilled knowledge

FSP matrix : Flow of DNN
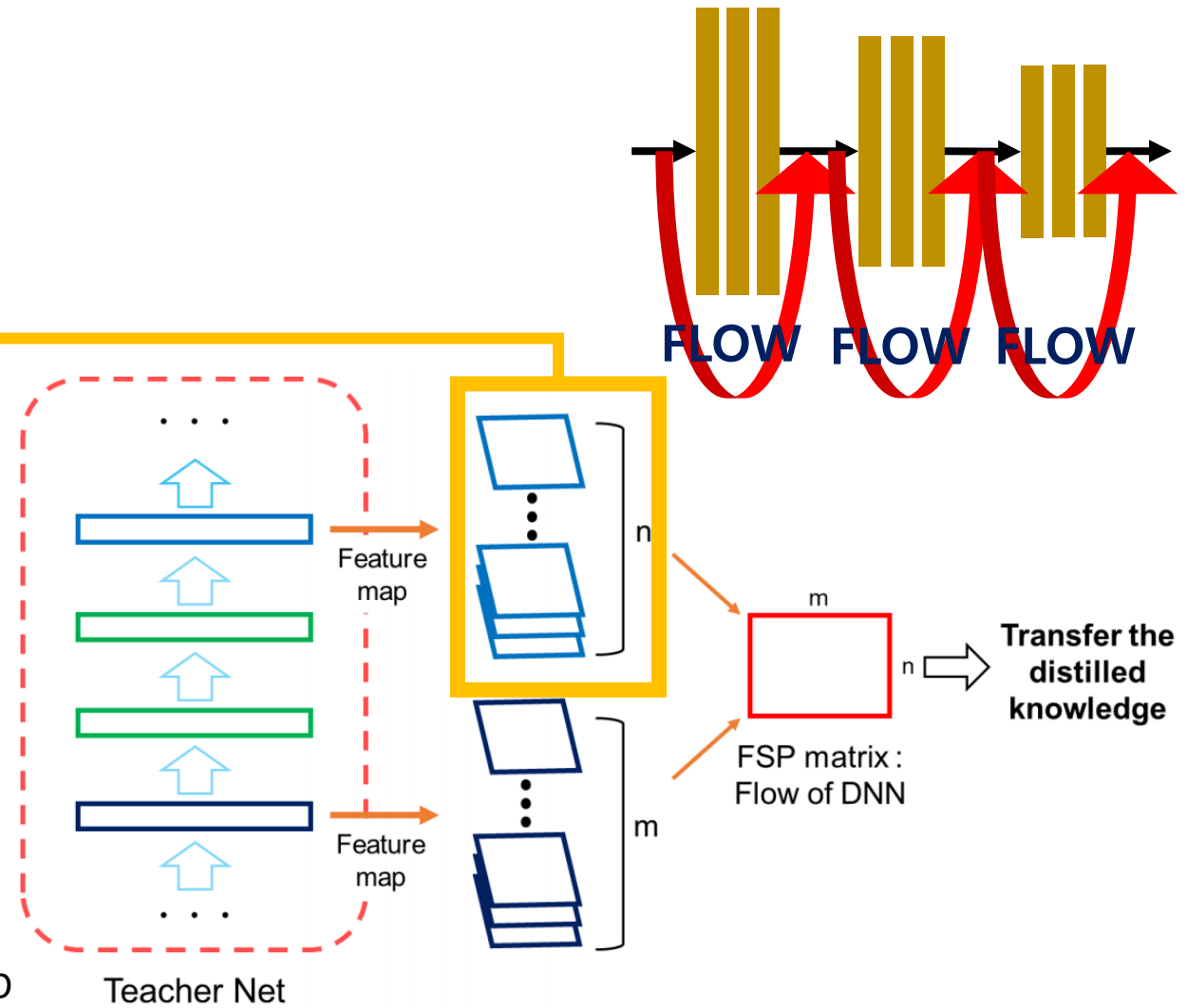
<Gram Matrix with across layers>

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A Gift from Knowledge Distillation: Fast Optimization, Network Minimization and Transfer Learning. In *CVPR*, 2017.

– Junho Yim, Donggyu Joo, Jihoon Bae and Junmo Kim.

$$G(a_1, \ldots, a_n, b_1, \ldots, b_m) = \begin{pmatrix} (a_1, b_1) & (a_1, b_2) & \cdots & (a_1, b_m) \\ (a_2, b_1) & (a_2, b_2) & \cdots & (a_2, b_m) \\ \vdots & \vdots & \ddots & \vdots \\ (a_n, b_1) & (a_n, b_2) & \cdots & (a_n, b_m) \end{pmatrix}$$
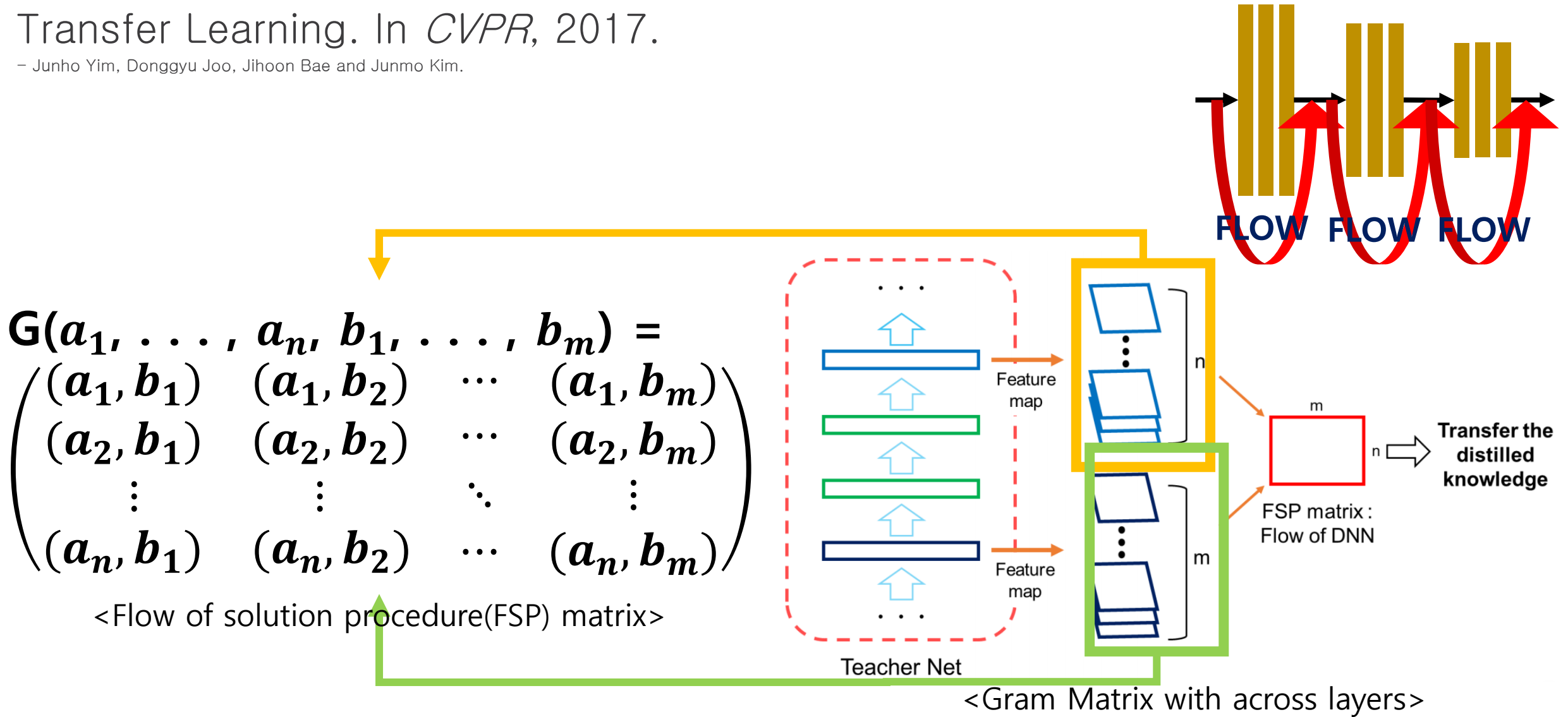
<Flow of solution procedure(FSP) matrix>

* (a, b) = Inner product of a and b

FLOW FLOW FLOW

Feature map

Feature map

Teacher Net

FSP matrix : Flow of DNN

Transfer the distilled knowledge

<Gram Matrix with across layers>

A Gift from Knowledge Distillation: Fast Optimization, Network Minimization and Transfer Learning. In *CVPR*, 2017.
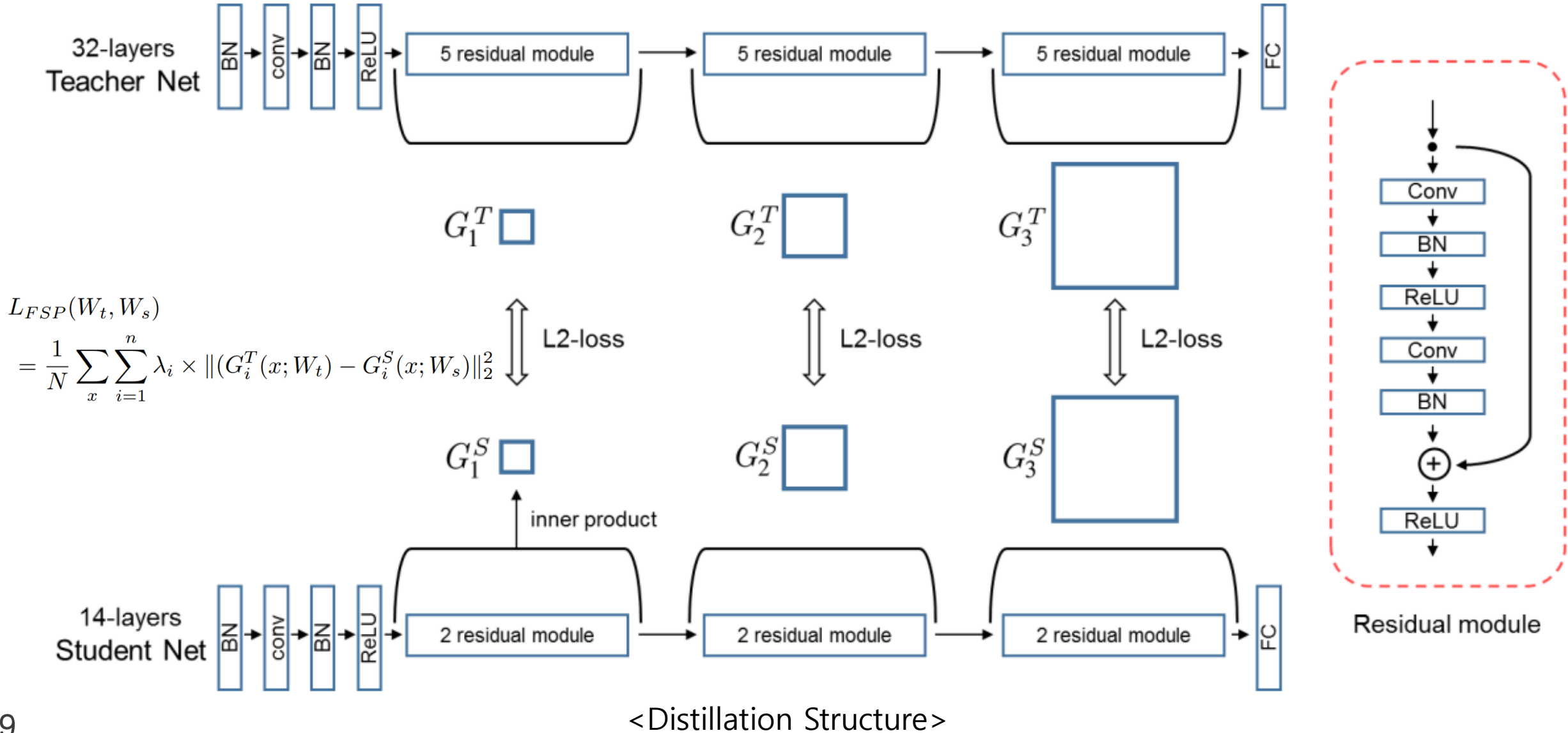
– Junho Yim, Donggyu Joo, Jihoon Bae and Junmo Kim.

$$L_{FSP}(W_t, W_s)$$
$$= \frac{1}{N} \sum_{x} \sum_{i=1}^{n} \lambda_i \times \|(G_i^T(x; W_t) - G_i^S(x; W_s)\|_2^2$$

<Distillation Structure>

A Gift from Knowledge Distillation: Fast Optimization, Network Minimization and Transfer Learning. In *CVPR*, 2017.

– Junho Yim, Donggyu Joo, Jihoon Bae and Junmo Kim.

	Accuracy
Teacher-original	91.91
Student-original	87.91
FitNet [20]	88.57
Proposed Method	88.70

Table 3. Recognition rates (%) on CIFAR-10. We used a residual DNN with 8 layers for the student DNN and 26 layers for the teacher DNN.

	Accuracy
Teacher-original	64.06
Student-original	58.65
FitNet [20]	61.28
Proposed Method	63.33

Table 4. Recognition rates (%) on CIFAR-100. We used a residual DNN with 14 layers for the student DNN and 32 layers for the teacher DNN.
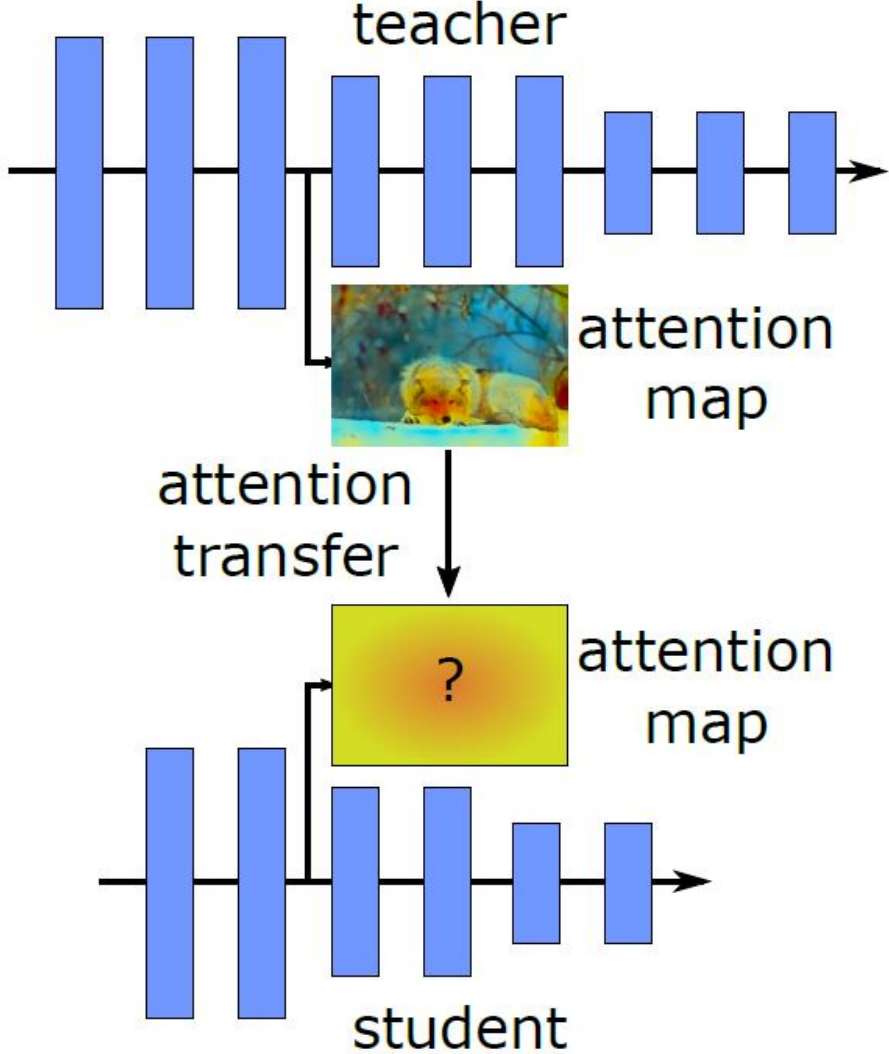
Paying More Attention to Attention: Improving the Performance of CNN via Attention Transfer
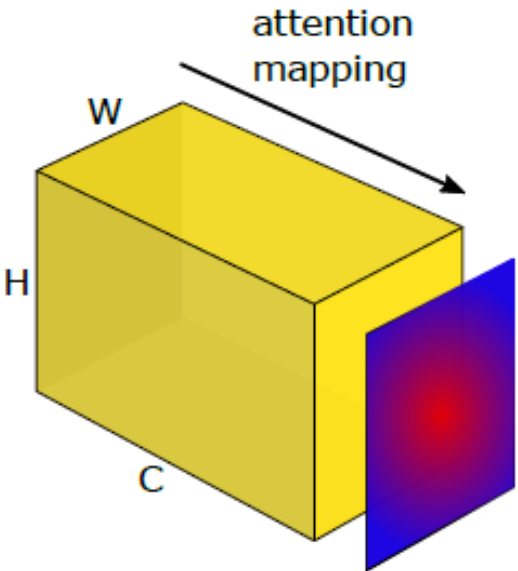
Paying More Attention to Attention: Improving the Performance of Convolutional Neural Networks via Attention Transfer. In *ICLR*, 2017.

– Sergey Zagoruyko and Nikos Komodakis.

<Normal image & Attention map>
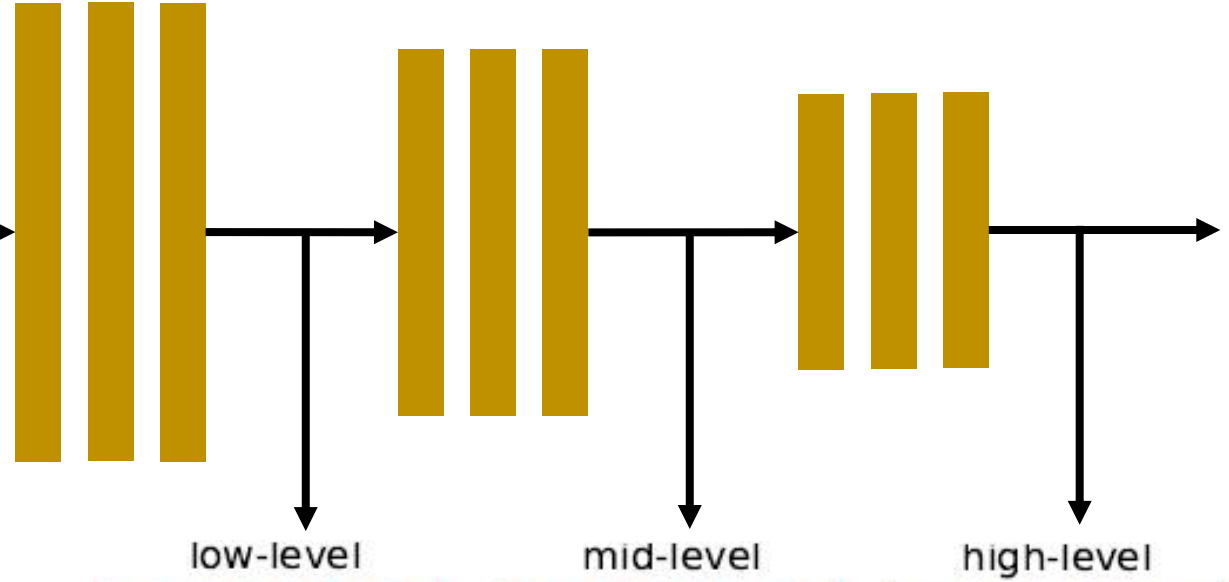
<Attention Transfer>

Paying More Attention to Attention: Improving the Performance of Convolutional Neural Networks via Attention Transfer. In *ICLR*, 2017.

– Sergey Zagoruyko and Nikos Komodakis.

attention map

attention mapping

$$\mathcal{F} : R^{C \times H \times W} \to R^{H \times W}$$
$$F_{\mathrm{sum}}(A) = \sum_{i=1}^{C} |A_i|$$
$$F_{\mathrm{sum}}^{p}(A) = \sum_{i=1}^{C} |A_i|^p$$
$$F_{\mathrm{max}}^{p}(A) = \max_{i=1,C} |A_i|^p$$

low-level
63 x 63

mid-level
32 x 32

high-level
8 x 8

<Feature characteristic of each layer>

<Attention mapping functions>

33
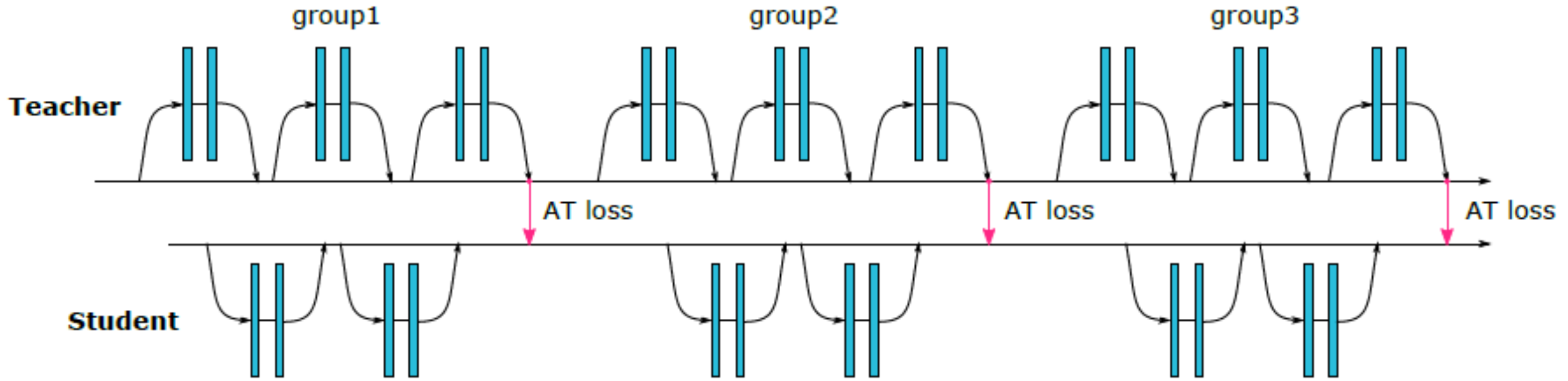
Paying More Attention to Attention: Improving the Performance of Convolutional Neural Networks via Attention Transfer. In *ICLR*, 2017.

– Sergey Zagoruyko and Nikos Komodakis.

$$\mathcal{L}_{AT} = \mathcal{L}(\mathbf{W}_S, x) + \frac{\beta}{2} \sum_{j \in \mathcal{I}} \| \frac{Q_S^j}{\|Q_S^j\|_2} - \frac{Q_T^j}{\|Q_T^j\|_2} \|_p$$

\<Attention Transfer structure\>

Paying More Attention to Attention: Improving the Performance of Convolutional Neural Networks via Attention Transfer. In *ICLR*, 2017.

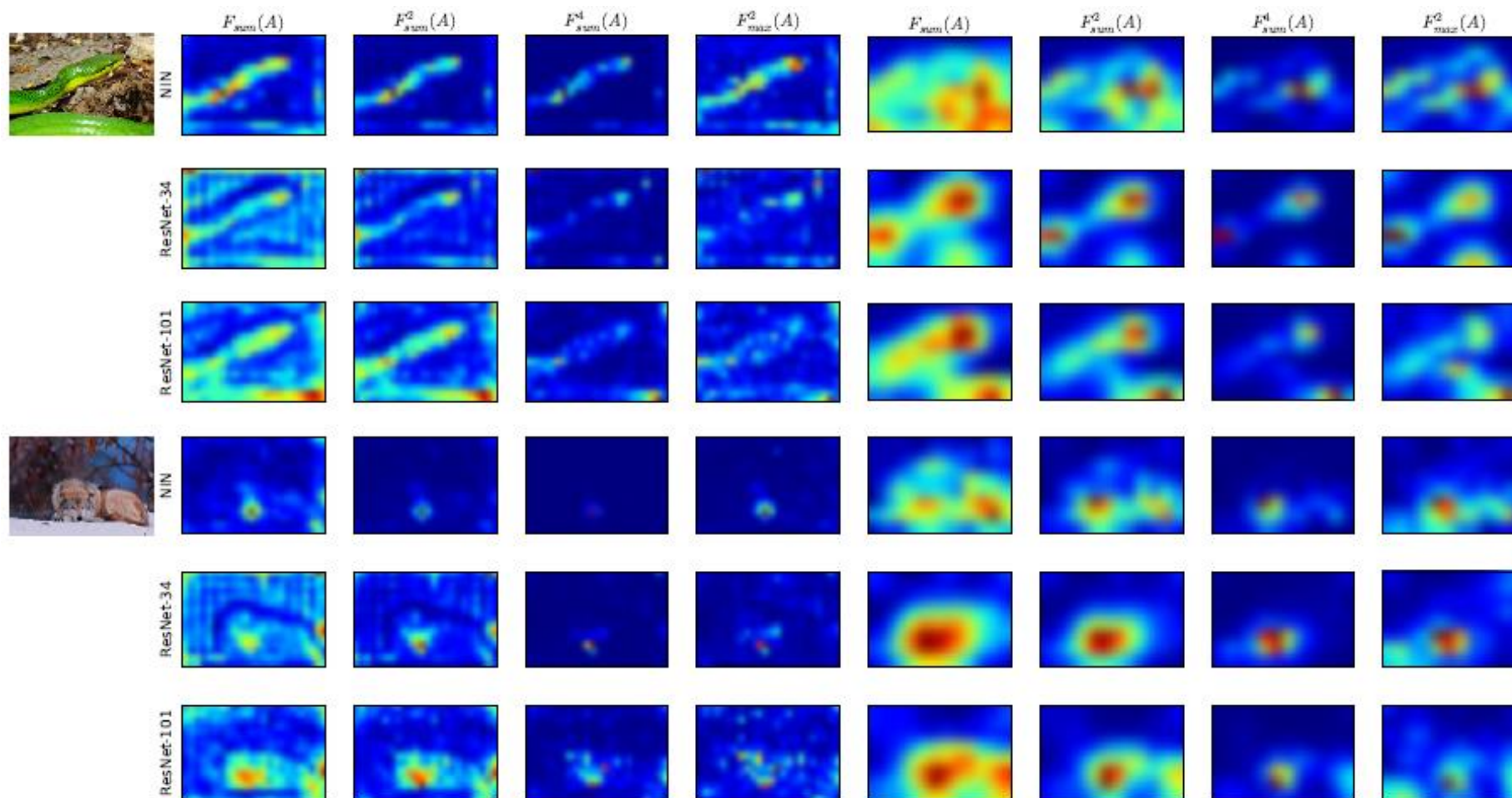– Sergey Zagoruyko and Nikos Komodakis.

Figure 4: Activation attention maps for various ImageNet networks: Network-In-Network (62% top-1 val accuracy), ResNet-34 (73% top-1 val accuracy), ResNet-101 (77.3% top-1 val accuracy). Left part: mid-level activations, right part: top-level pre-softmax acivations

Paying More Attention to Attention: Improving the Performance of Convolutional Neural Networks via Attention Transfer. In *ICLR*, 2017.

— Sergey Zagoruyko and Nikos Komodakis.

student	teacher	student	AT	F-ActT	KD	AT+KD	teacher
NIN-thin, 0.2M	NIN-wide, 1M	9.38	8.93	9.05	8.55	8.33	7.28
WRN-16-1, 0.2M	WRN-16-2, 0.7M	8.77	7.93	8.51	7.41	7.51	6.31
WRN-16-1, 0.2M	WRN-40-1, 0.6M	8.77	8.25	8.62	8.39	8.01	6.58
WRN-16-2, 0.7M	WRN-40-2, 2.2M	6.31	5.85	6.24	6.08	5.71	5.23

Table 1: Activation-based attention transfer (AT) with various architectures on CIFAR-10. Error is computed as median of 5 runs with different seed. F-ActT means full-activation transfer (see §4.1.2).

Model	top1, top5
ResNet-18	30.4, 10.8
AT	29.3, 10.0
ResNet-34	26.1, 8.3

Table 5: Attention transfer validation error (single crop) on ImageNet. Transfer losses are added on epoch 60/100.
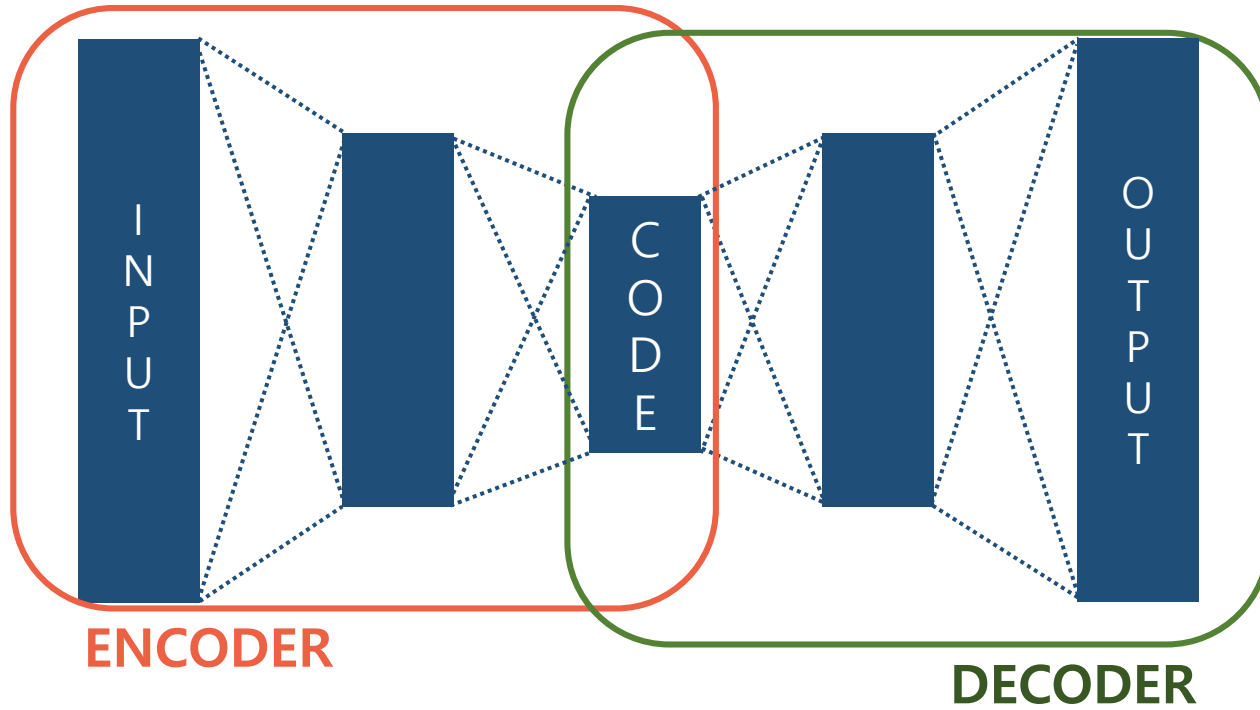
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Paraphrasing Complex Network: Network Compression via Factor Transfer

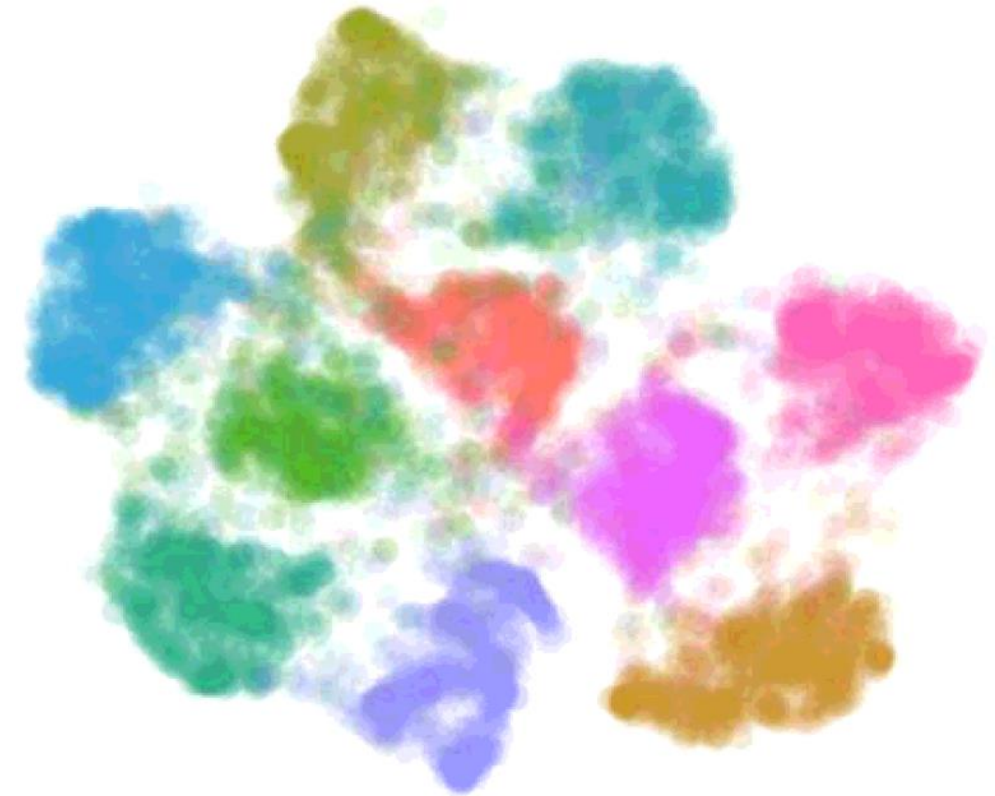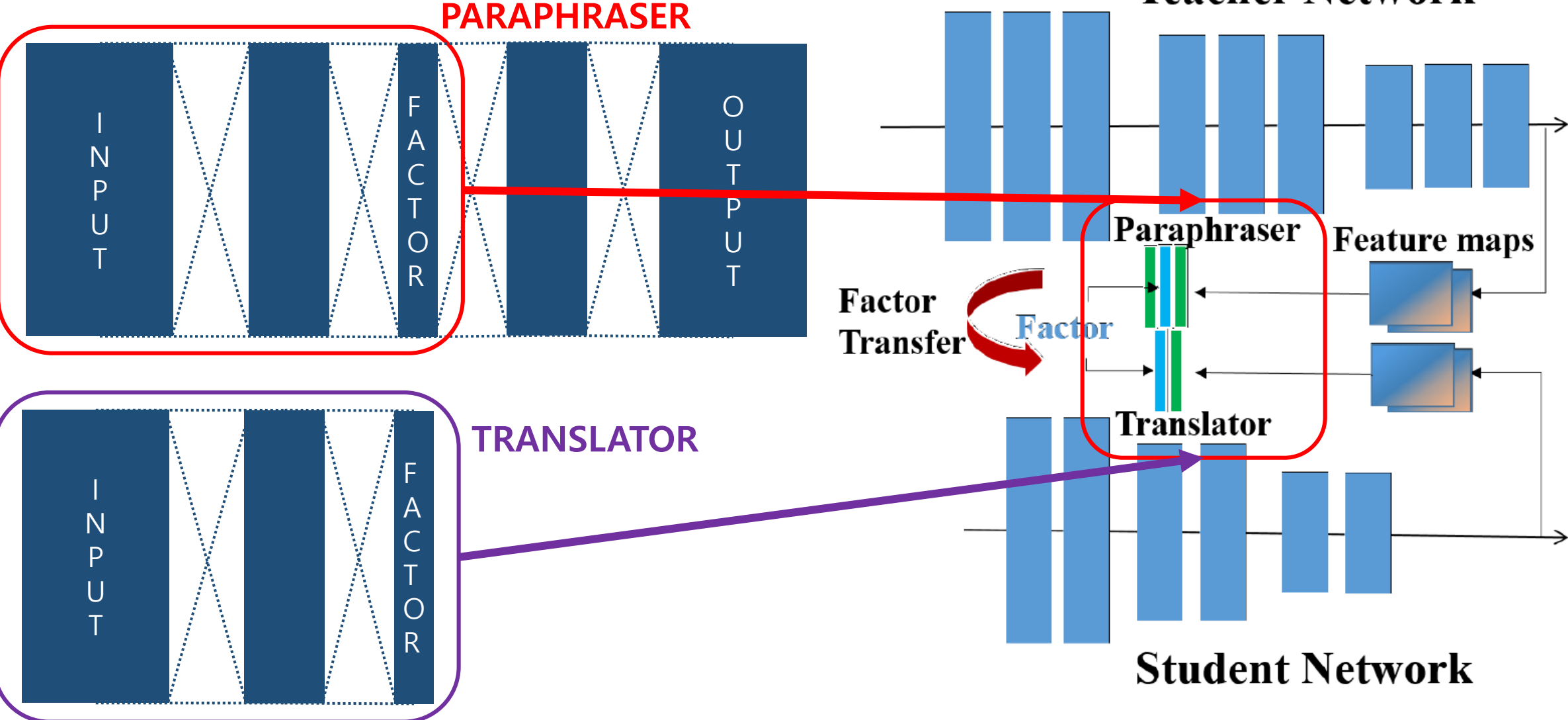# Paraphrasing Complex Network: Network Compression via Factor Transfer.
In *NIPS*, 2018.

– Jangho Kim, SeongUk Park and Nojun Kwak.

<Autoencoder structure>

<t-SNE visualization of factor space>

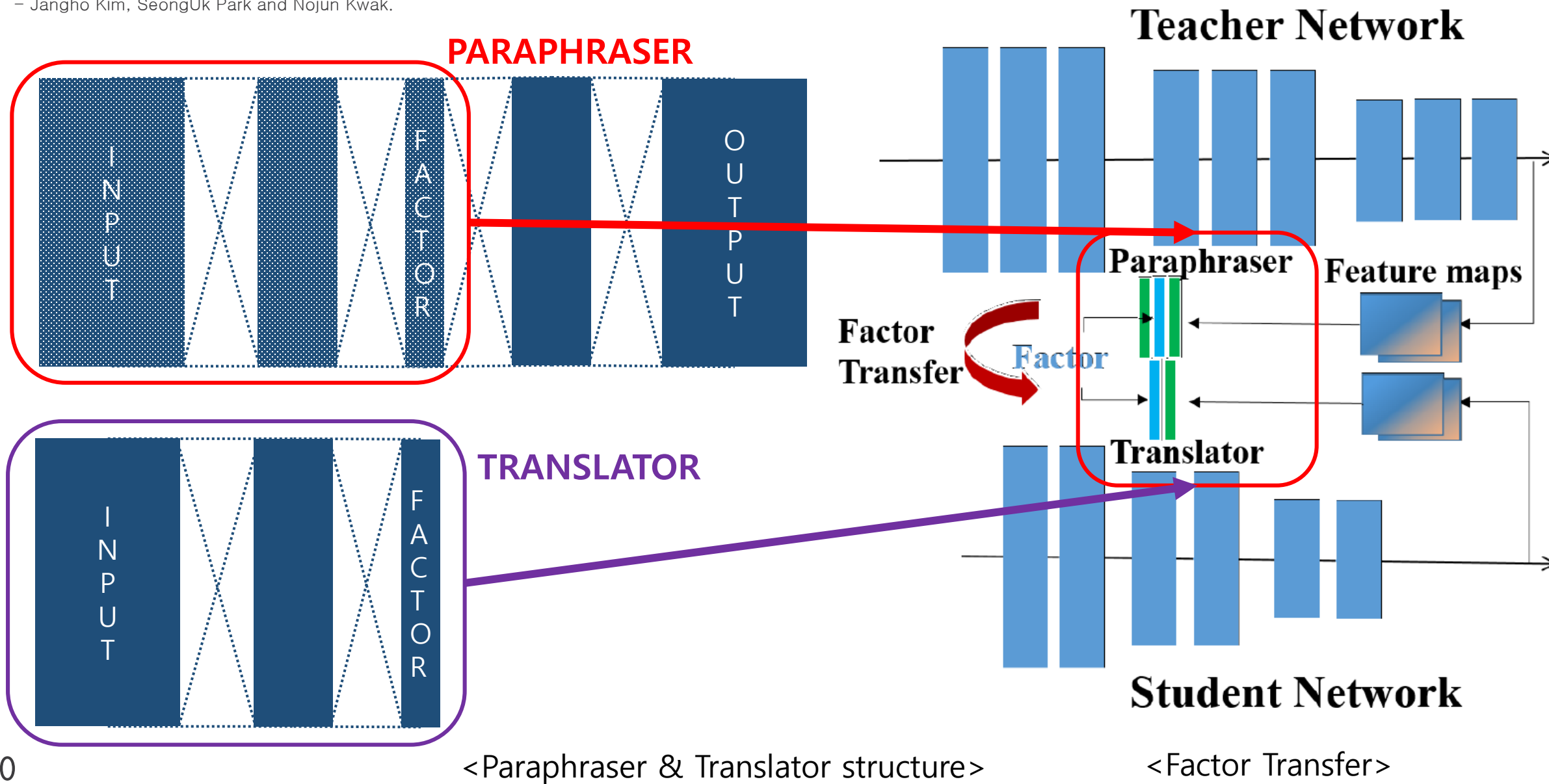# Paraphrasing Complex Network: Network Compression via Factor Transfer.
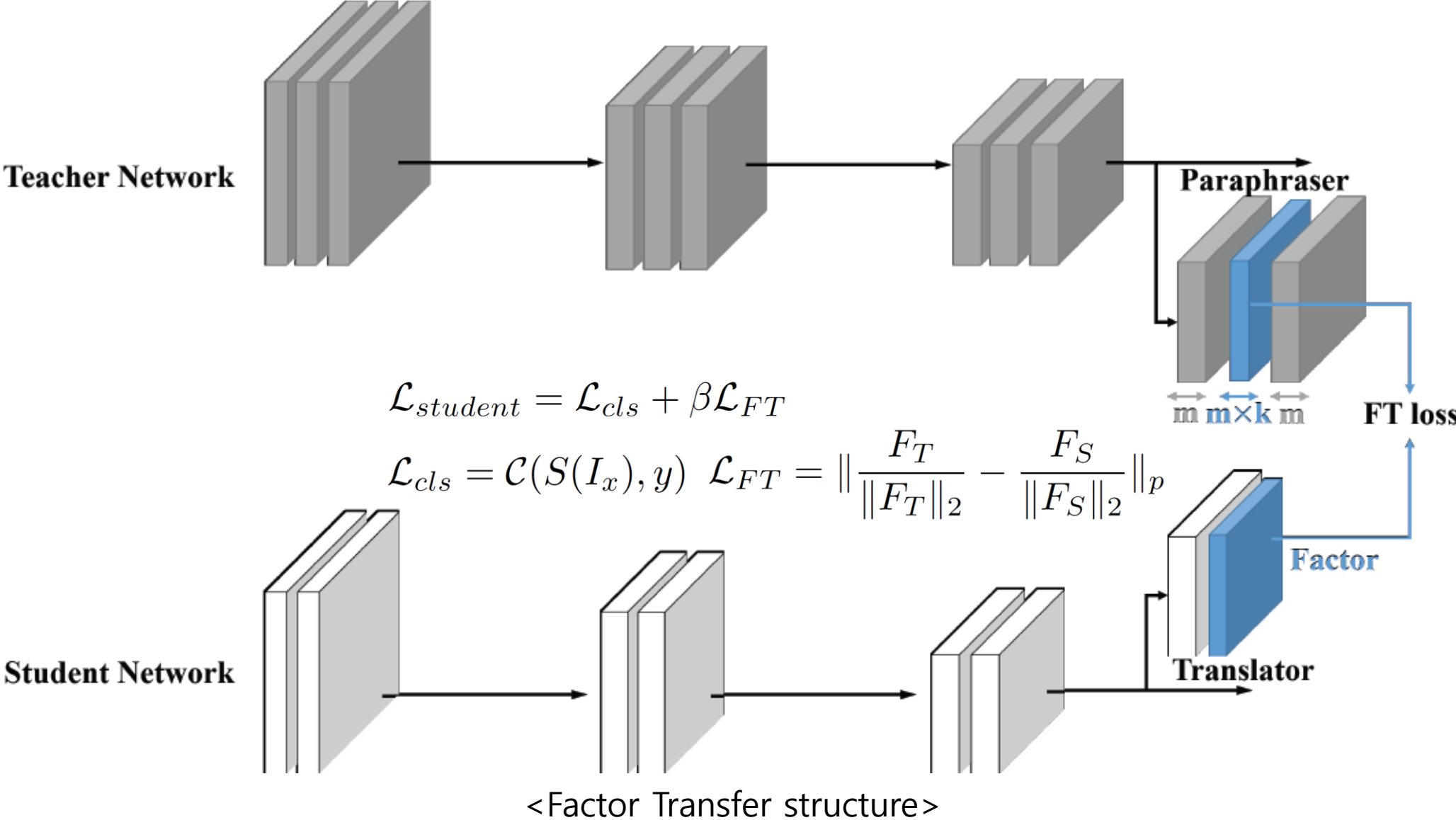## In *NIPS*, 2018.

– Jangho Kim, SeongUk Park and Nojun Kwak.

PARAPHRASER

TRANSLATOR

Teacher Network

Factor Transfer

Factor

Paraphraser

Feature maps

Translator

Student Network

39

<Paraphraser & Translator structure>

<Factor Transfer>

Paraphrasing Complex Network: Network Compression via Factor Transfer. In *NIPS*, 2018.

– Jangho Kim, SeongUk Park and Nojun Kwak.

PARAPHRASER

TRANSLATOR

Teacher Network

Paraphraser

Feature maps

Factor Transfer

Factor

Translator

Student Network

<Paraphraser & Translator structure>   <Factor Transfer>

Paraphrasing Complex Network: Network Compression via Factor Transfer. In *NIPS*, 2018.

– Jangho Kim, SeongUk Park and Nojun Kwak.

$$\mathcal{L}_{student} = \mathcal{L}_{cls} + \beta\mathcal{L}_{FT}$$

$$\mathcal{L}_{cls} = \mathcal{C}(S(I_x), y) \quad \mathcal{L}_{FT} = \|\frac{F_T}{\|F_T\|_2} - \frac{F_S}{\|F_S\|_2}\|_p$$

<Factor Transfer structure>

Paraphrasing Complex Network: Network Compression via Factor Transfer. In *NIPS*, 2018.

– Jangho Kim, SeongUk Park and Nojun Kwak.

Student	Teacher	Student	AT	KD	FT	AT+KD	FT+KD	Teacher
ResNet-56 (0.85M)	ResNet-110 (1.73M)	28.04	27.28	27.96	**25.62**	28.01	26.93	26.91
ResNet-20 (0.27M)	ResNet-110 (1.73M)	31.24	31.04	33.14	**29.08**	34.78	32.19	26.91

Student	Teacher	$k = 0.5$	$k = 0.75$	$k = 1$	$k = 2$	$k = 4$	CAE	RAE
ResNet-56 (0.85M)	ResNet-110 (1.73M)	**25.62**	25.78	25.85	25.63	25.87	26.41	26.29
ResNet-20 (0.27M)	ResNet-110 (1.73M)	29.20	29.25	29.28	29.19	**29.08**	29.84	30.11

Table 3: Mean classification error (%) on CIFAR-100 dataset (5 runs). All the numbers are from our implementation.

Paraphraser	Translator	CIFAR-10	CIFAR-100
Yes	No	6.18	27.61
No	Yes	6.12	27.39
Yes	Yes	5.71	26.91
Student (WRN-40-1[0.6M])		7.02	28.81
Teacher (WRN-40-2[2.2M])		4.96	24.10

Table 4: Ablation study with and without the paraphraser ($k = 0.5$) and the Translator. (Mean test error (%) of 5 runs).
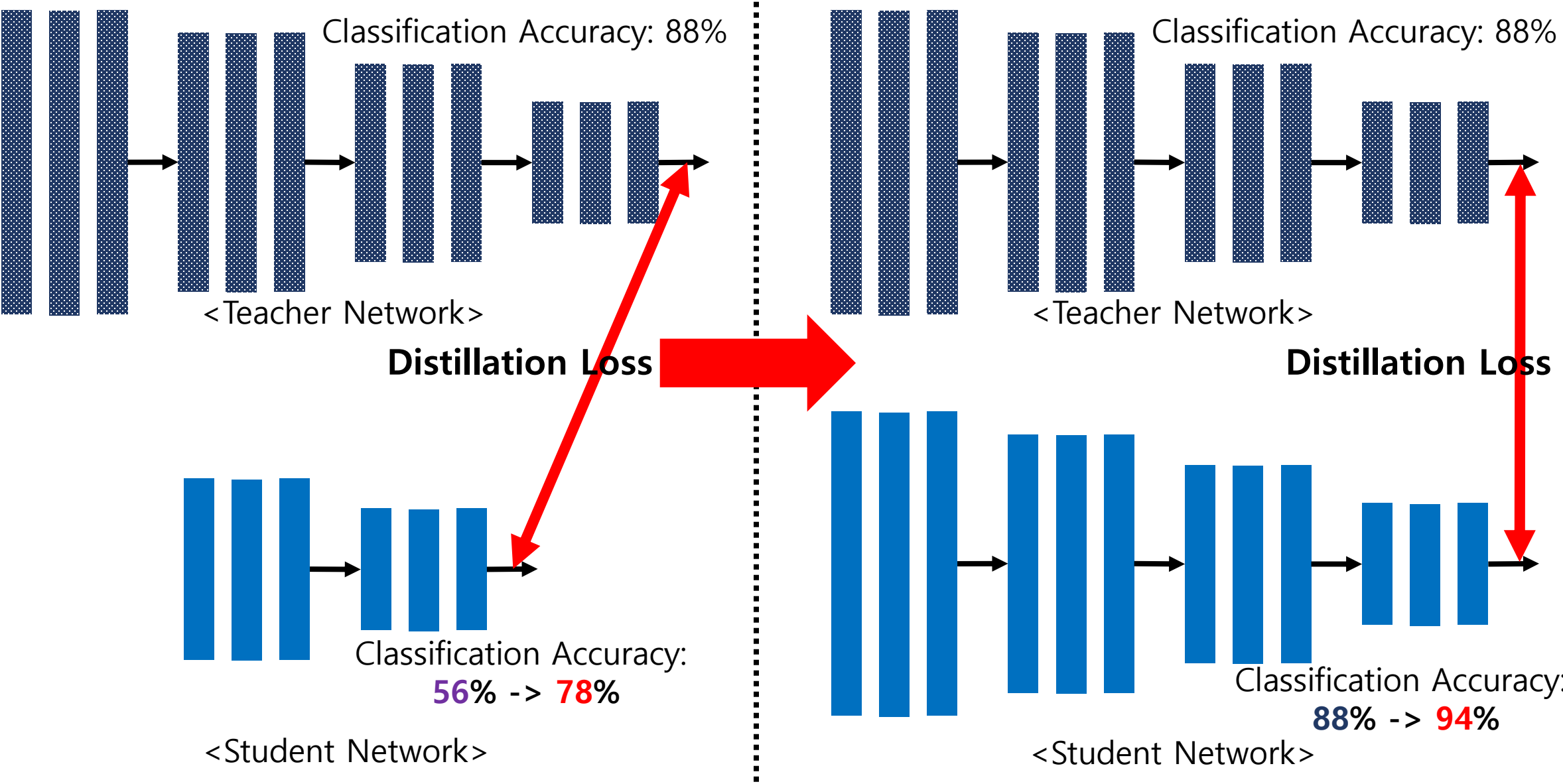
Method	Network	Top-1	Top-5
Student	Resnet-18	29.91	10.68
KD	Resnet-18	33.83	12.55
AT	Resnet-18	29.36	10.23
FT ($k = 0.5$)	Resnet-18	**28.57**	**9.71**
Teacher	Resnet-34	26.73	8.57

Table 5: Top-1 and Top-5 classification error (%) on ImageNet dataset. All the numbers are from our implementation.
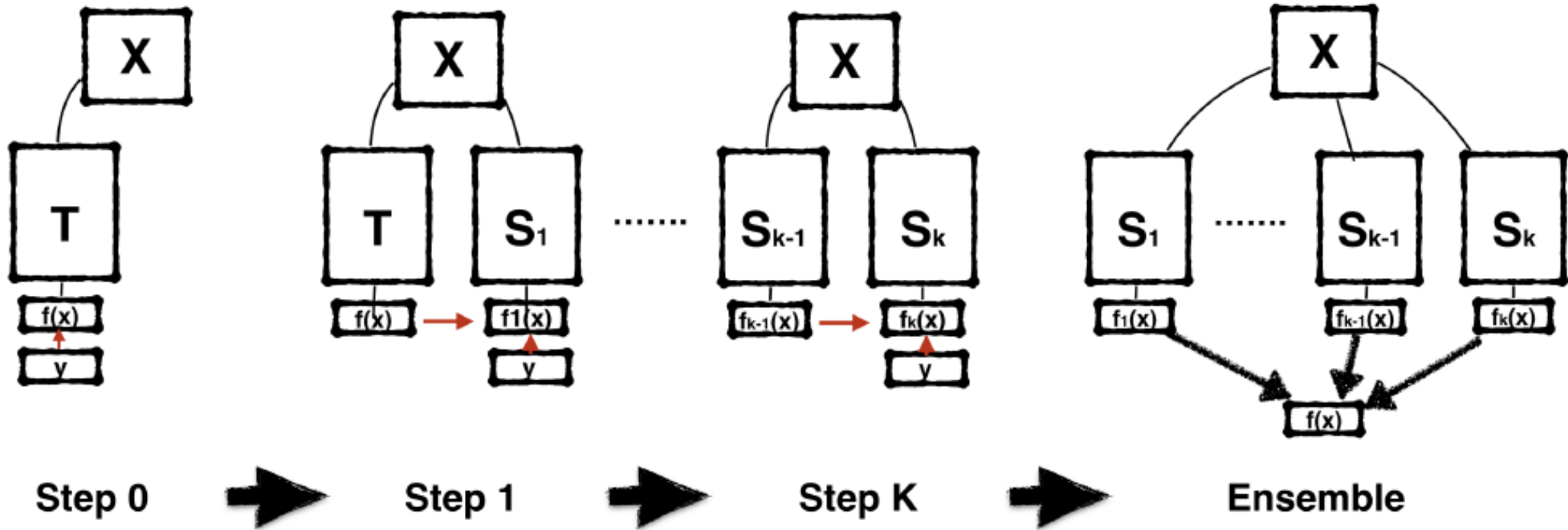
Born-Again Neural Networks

2018
ICML

Born-Again Neural Networks. In *ICML*, 2018.

– Tommaso Furlanello, Zachary C. Lipton, Michael Tschannen, Laurent Itti and Anima Anandkumar.

Classification Accuracy: 88%

<Teacher Network>

Distillation Loss

Classification Accuracy:
56% -> **78**%

<Student Network>

Classification Accuracy: 88%

<Teacher Network>

Distillation Loss

Classification Accuracy:
88% -> **94**%

<Student Network>

Born–Again Neural Networks. In *ICML*, 2018.

– Tommaso Furlanello, Zachary C. Lipton, Michael Tschannen, Laurent Itti and Anima Anandkumar.

Figure 1. **Graphical representation of the BAN training procedure**: during the first step the teacher model T is trained from the labels Y. Then, at each consecutive step, a new identical model is initialized from a different random seed and trained from the supervision of the earlier generation. At the end of the procedure, additional gains can be achieved with an ensemble of multiple students generations.

$$\mathcal{L}(f(x, \arg\min_{\theta_{k-1}} \mathcal{L}(f(x, \theta_{k-1}))), f(x, \theta_k)) \qquad \hat{f}^k(x) = \sum_{i=1}^{k} f(x, \theta_i)/k$$

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Born–Again Neural Networks. In *ICML*, 2018.
– Tommaso Furlanello, Zachary C. Lipton, Michael Tschannen, Laurent Itti and Anima Anandkumar.

Table 1. **Test error on CIFAR-10** for Wide-ResNet with different depth and width and DenseNet of different depth and growth factor.

Network	Parameters	Teacher	BAN
Wide-ResNet-28-1	0.38 M	6.69	**6.64**
Wide-ResNet-28-2	1.48 M	5.06	**4.86**
Wide-ResNet-28-5	9.16 M	4.13	**4.03**
Wide-ResNet-28-10	36 M	**3.77**	3.86
DenseNet-112-33	6.3 M	3.84	**3.61**
DenseNet-90-60	16.1 M	3.81	**3.5**
DenseNet-80-80	22.4 M	**3.48**	3.49
DenseNet-80-120	50.4 M	**3.37**	3.54

Table 3. **Test error on CIFAR-100** for Wide-ResNet students trained from identical Wide-ResNet teachers and for DenseNet-90-60 students trained from Wide-ResNet teachers

Network	Teacher	BAN	Dense-90-60
Wide-ResNet-28-1	30.05	29.43	24.93
Wide-ResNet-28-2	25.32	24.38	18.49
Wide-ResNet-28-5	20.88	20.93	17.52
Wide-ResNet-28-10	19.08	18.25	16.79

Network Recasting:
A Universal Method for Network Architecture Transformation

2019
AAAI

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.
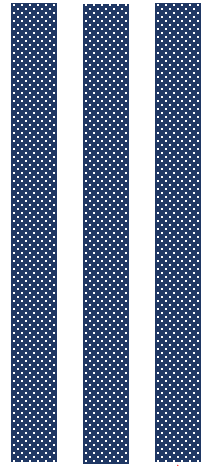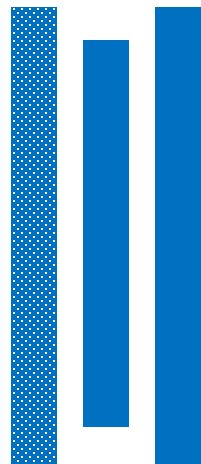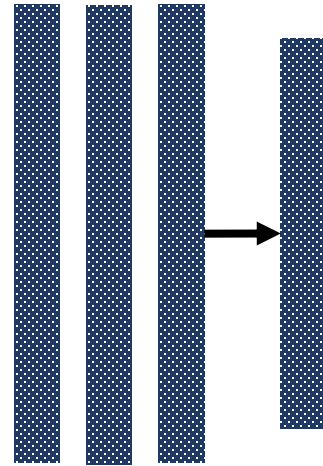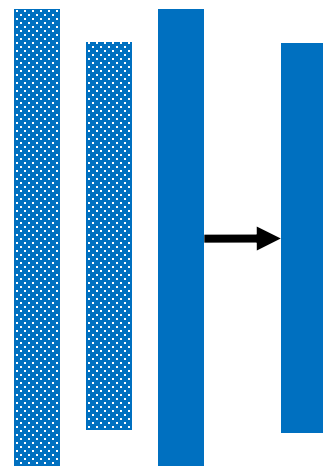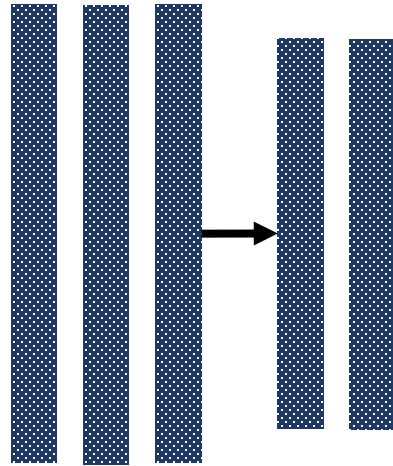
– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

Number of layers

Number of channels

Classification Accuracy: 88%

<Teacher Network>

Distillation Loss

Classification Accuracy:
56% -> **78**%

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.
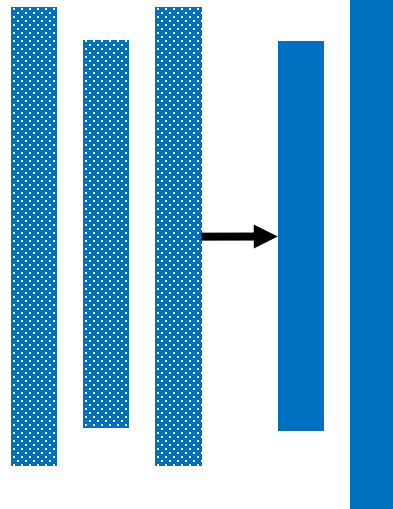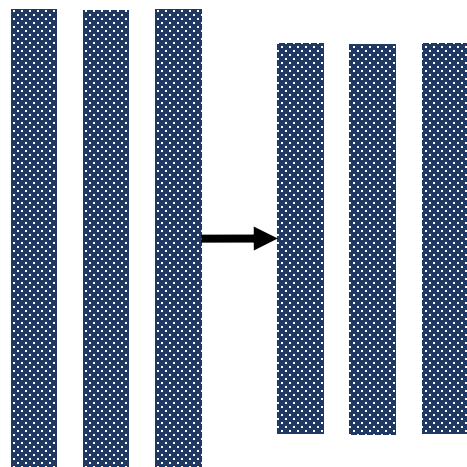
<Teacher Network>

MSE Loss

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

<Teacher Network>

MSE Loss

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

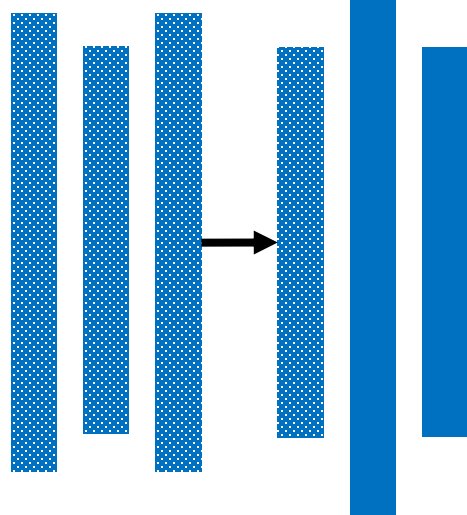– Joonsang Yu, Sungbum Kang and Kiyoung Choi.
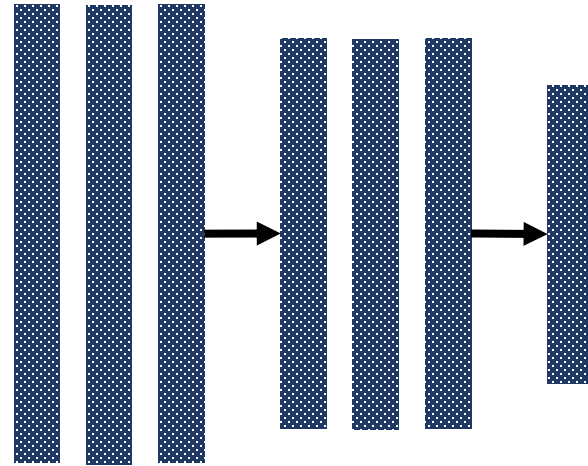

<Teacher Network>

MSE Loss

<Student Network>

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.
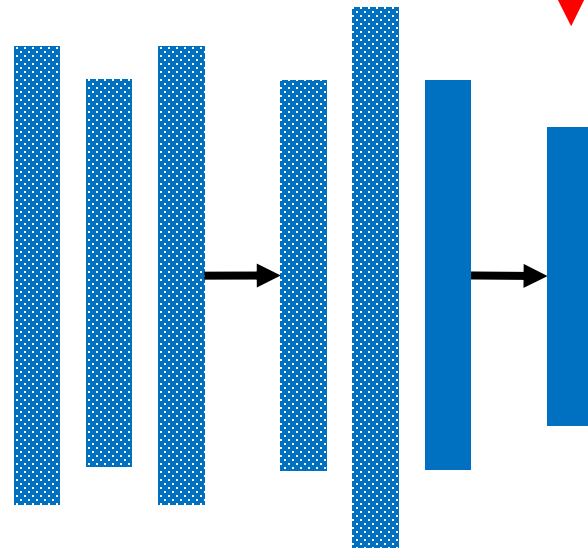
<Teacher Network>

MSE Loss

<Student Network>

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N} \|A(x; W_T) - A(x; W_S)\|_2^2$$
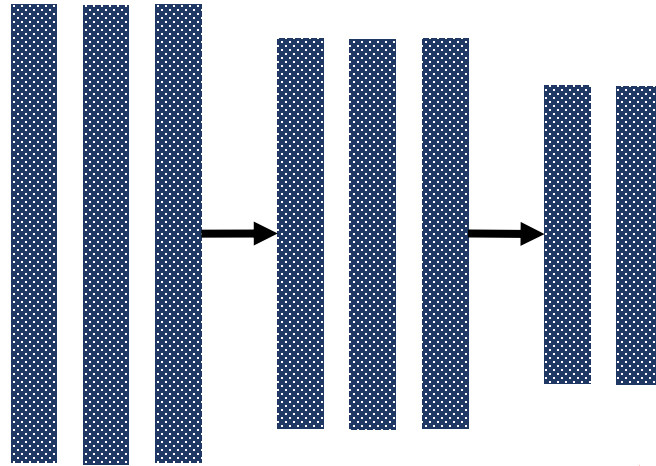
Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

<Teacher Network>

MSE Loss

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

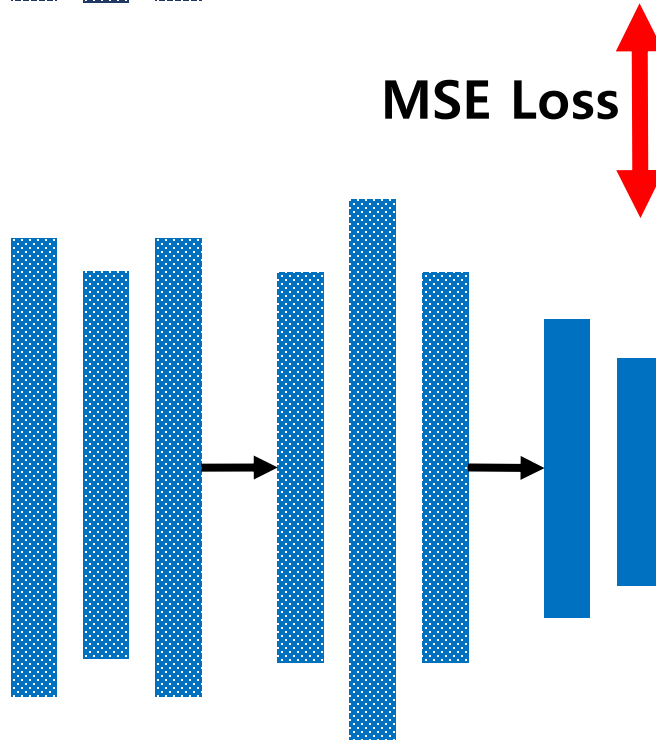– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

<Teacher Network>

<Student Network>

MSE Loss

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N} \|A(x; W_T) - A(x; W_S)\|_2^2$$

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

<Teacher Network>

MSE Loss

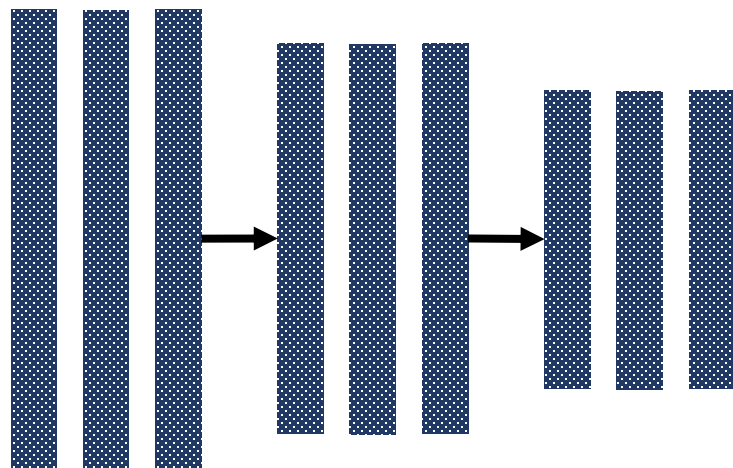$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation.
In *AAAI*, 2019.

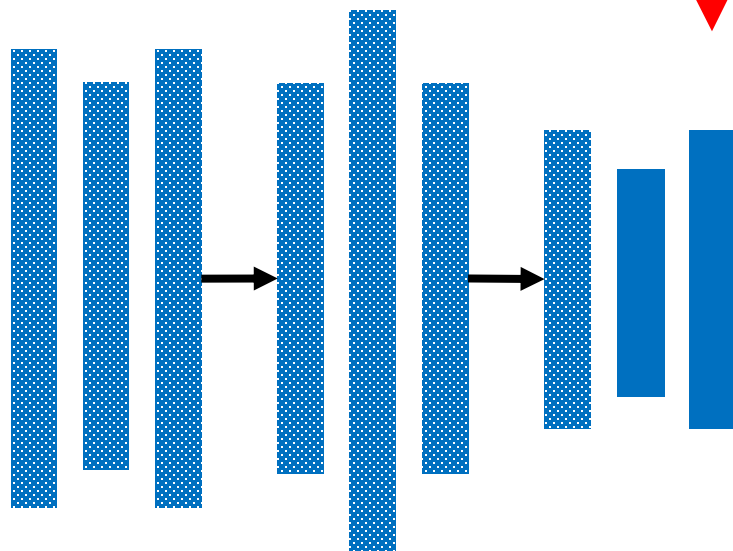– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

<Teacher Network>

MSE Loss

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

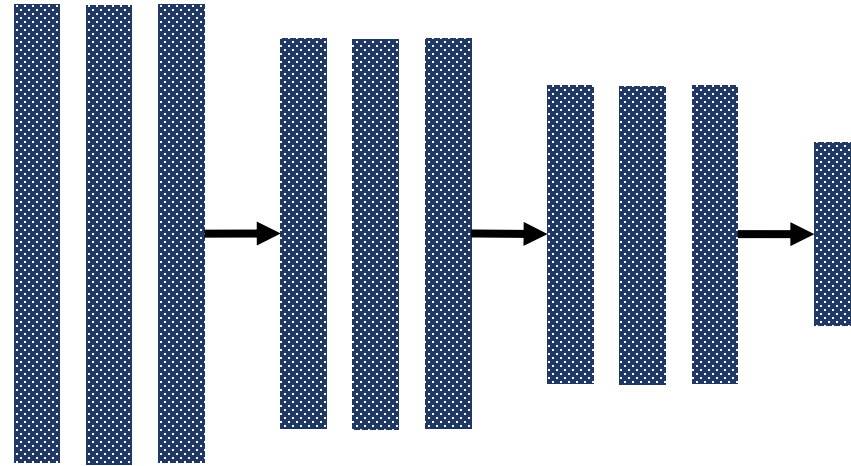<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.
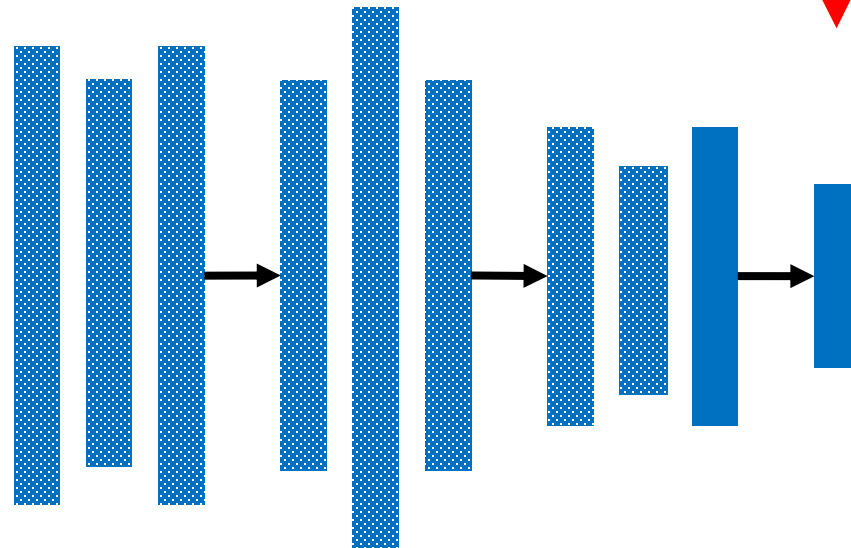

<Teacher Network>

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N} \|A(x; W_T) - A(x; W_S)\|_2^2$$

MSE Loss

<Student Network>
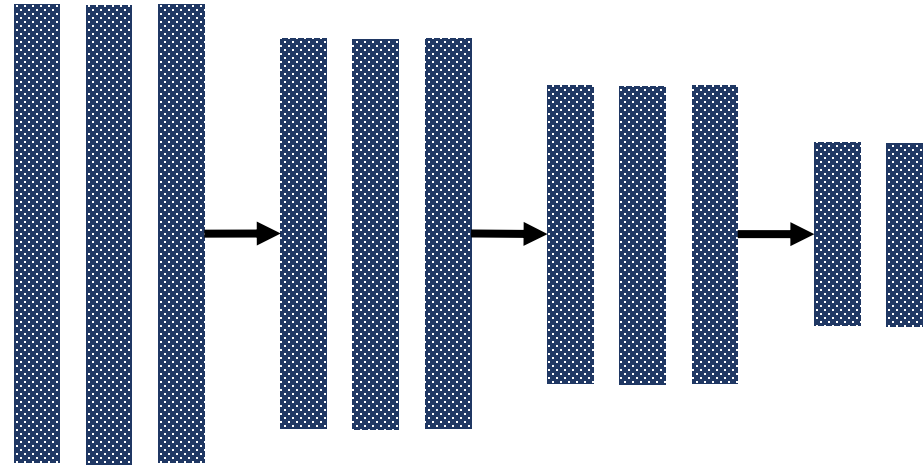
Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

<Teacher Network>

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

MSE Loss

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

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<Teacher Network>

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

MSE Loss

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

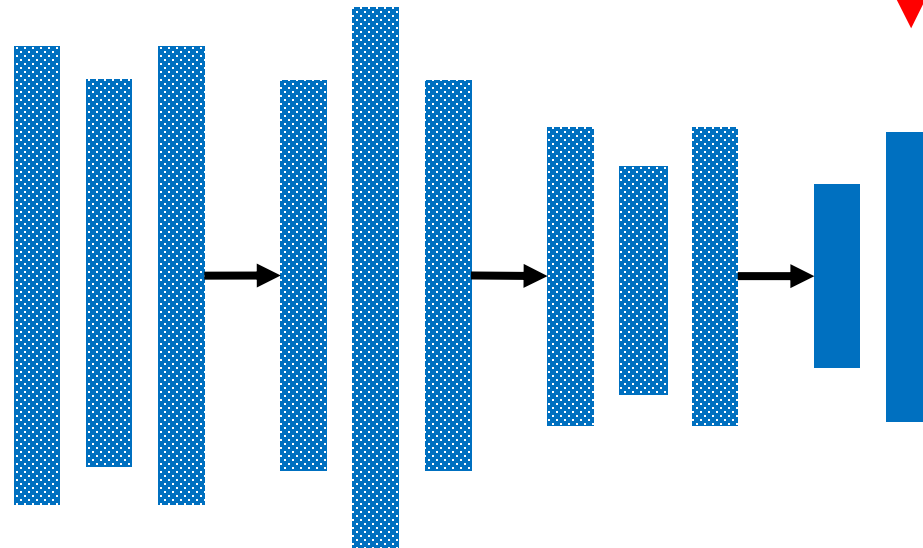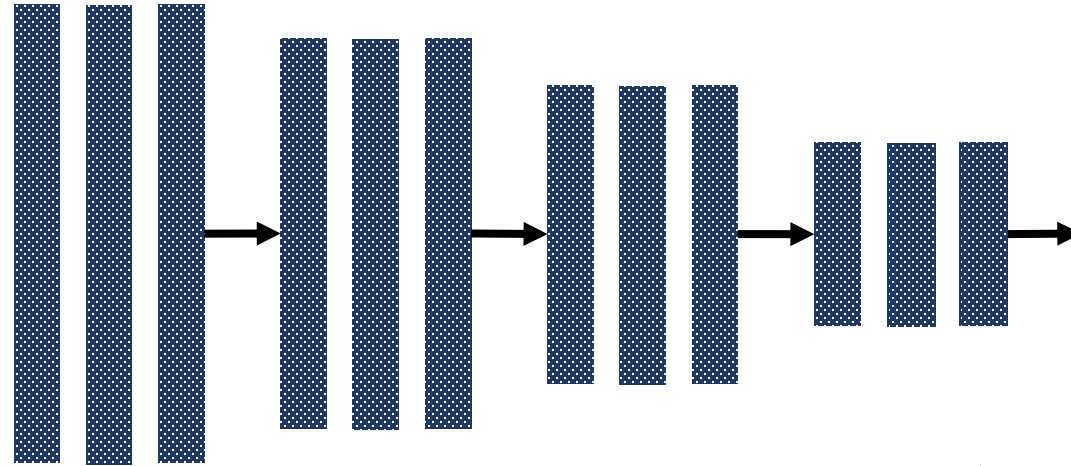– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

<Teacher Network>

$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2$$

MSE Loss

<Student Network>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

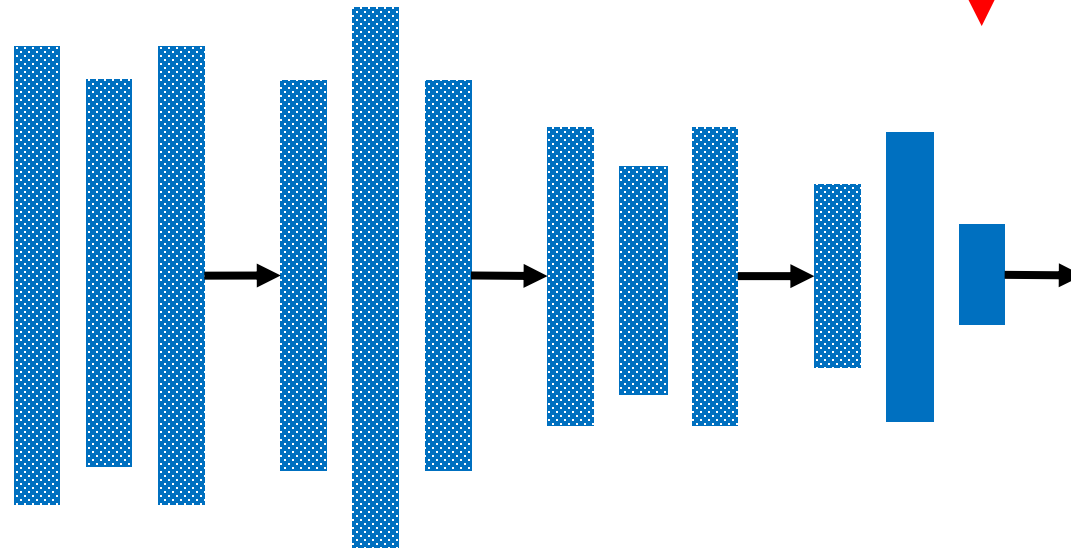– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

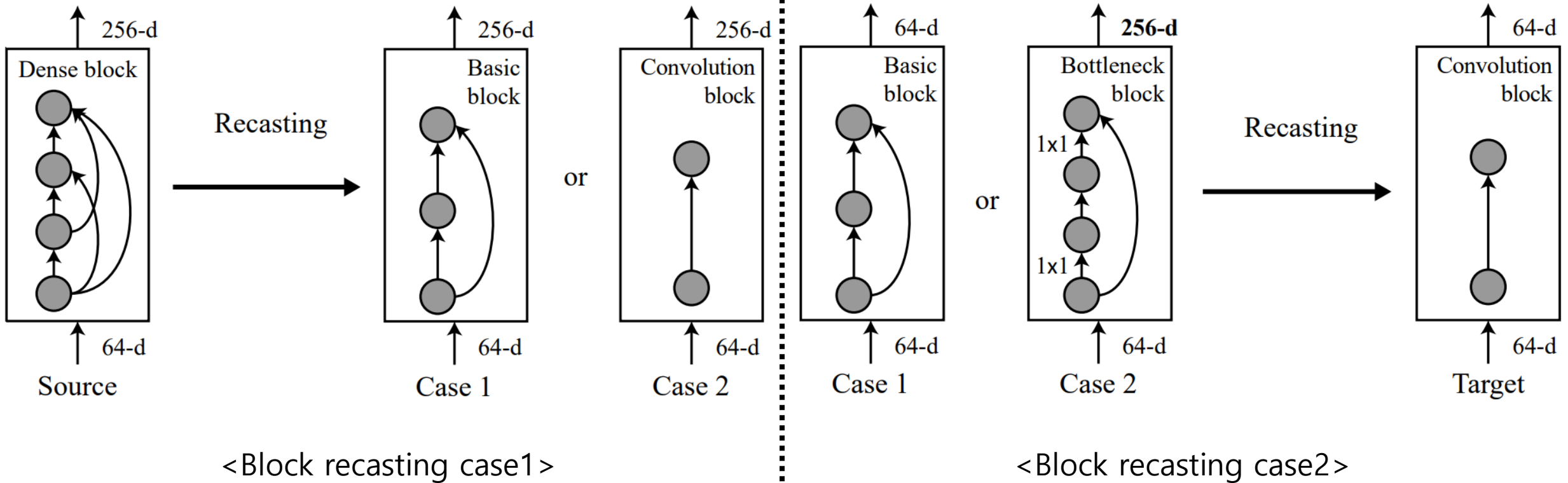<Block recasting case1>   <Block recasting case2>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

Recasting Type	Source	Target	Dimension
Transformation	Dense	Basic	Preserved
	Dense	Convolution	Preserved
	Basic	Convolution	Preserved
	Bottleneck	Convolution	Reduced
Compression	Basic	Basic	Reduced
	Convolution	Convolution	Reduced

\<Method for dimension mismatch\>   \<Recasting Methods\>

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

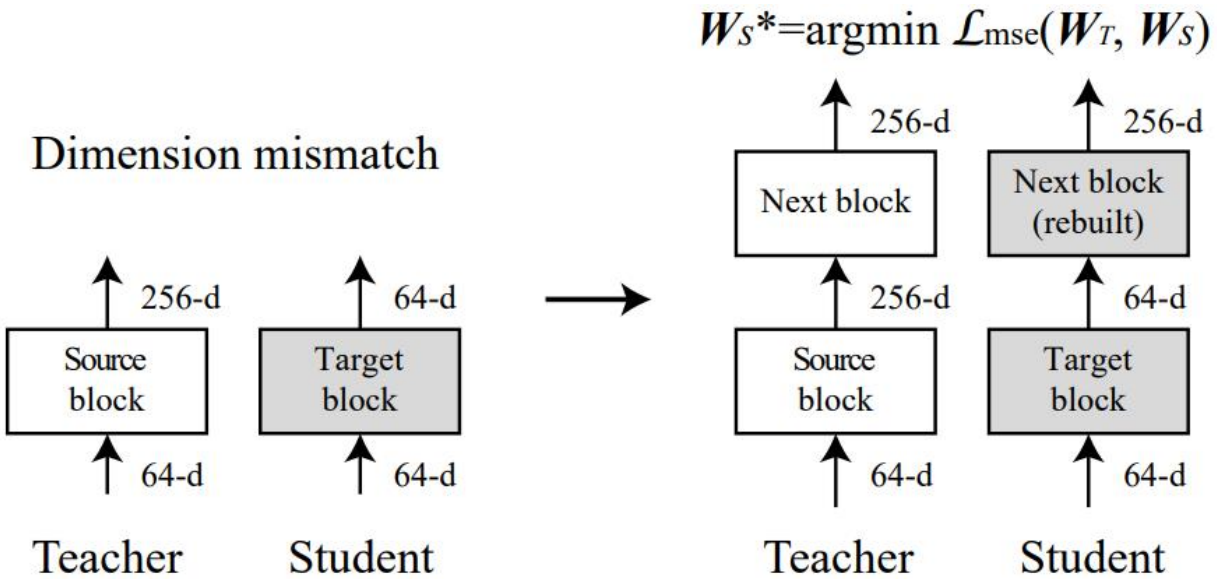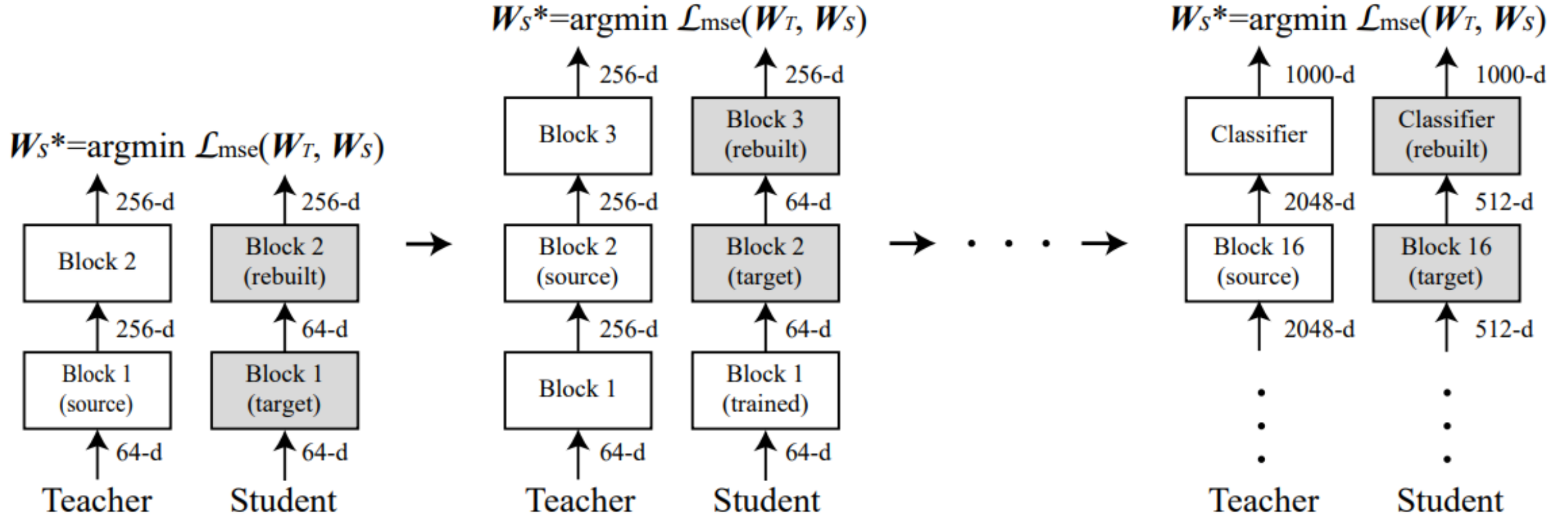$$\mathcal{L}_{mse}(W_T, W_S) = \frac{1}{N}\|A(x; W_T) - A(x; W_S)\|_2^2 \quad \mathcal{L}_{kd}(W_T, W_S) = \mathcal{L}_{mse\_logit}(W_T, W_S) + \mathcal{L}_{ce}(y_{true}, W_S)$$
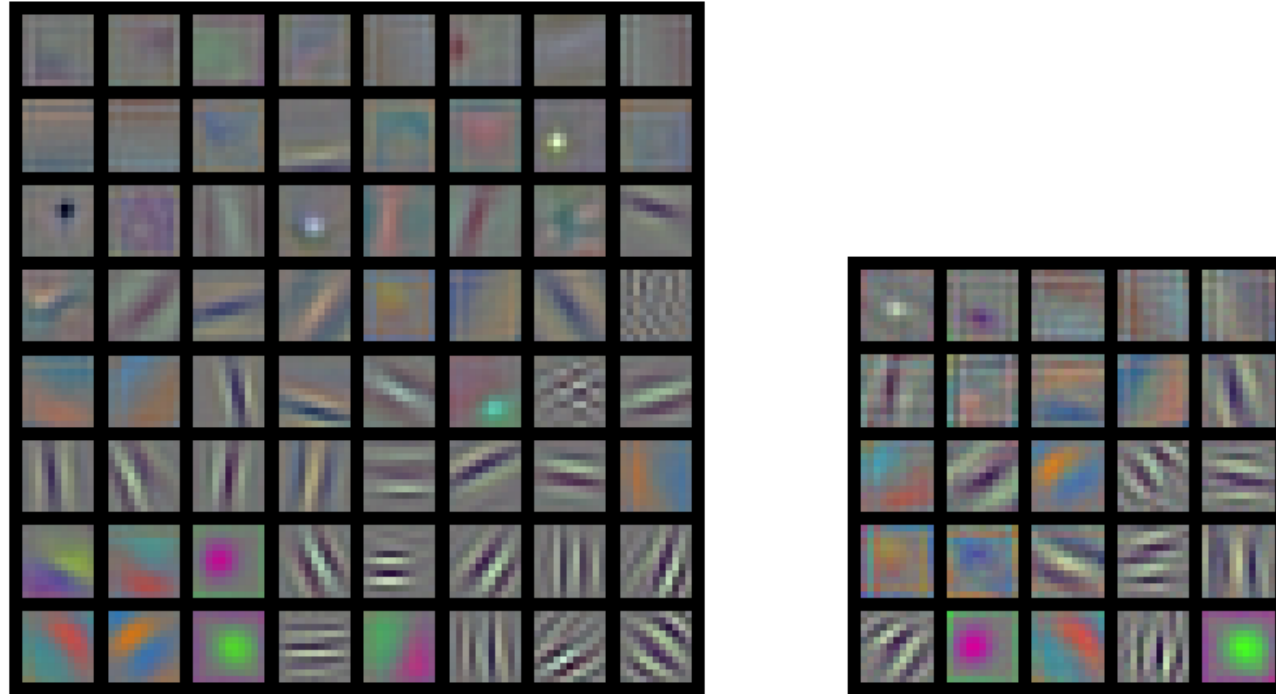
\<Network recasting structure\>

Figure 6: Visualization of filters in the first layer of AlexNet (*left*) and a student network (*right*). Redundant filters are removed after network recasting.

Network Recasting: A Universal Method for Network Architecture Transformation. In *AAAI*, 2019.

– Joonsang Yu, Sungbum Kang and Kiyoung Choi.

Table 3: Error rates (%) of compression results on CIFAR datasets. (B/M: billion/million)

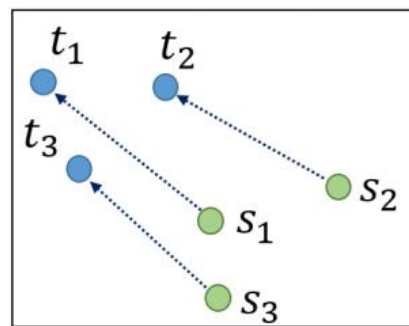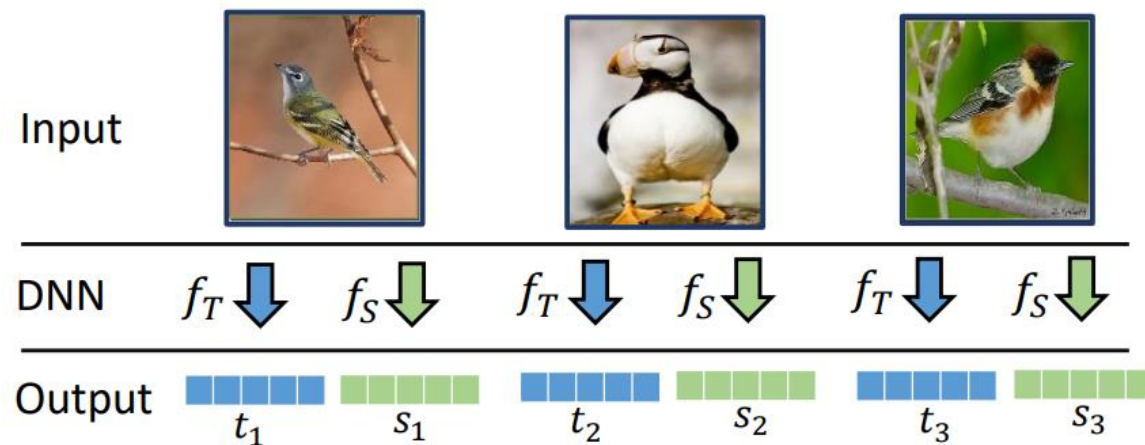| Method	Type	C10+	C100+	Params	Mults	Acts/image	Time/image
VGG-16							
Baseline		6.85	28.80	14.71M (1.0×)	313.20M (1.0×)	0.31M (1.0×)	0.37ms
Recasting	Conv	**8.31**	**31.56**	2.36M (6.2×)	50.63M (6.2×)	0.13M (2.4×)	0.31ms
KD	Conv	9.24	33.14	2.36M (6.2×)	50.63M (6.2×)	0.13M (2.4×)	0.31ms
Backprop	Conv	8.71	35.13	2.36M (6.2×)	50.63M (6.2×)	0.13M (2.4×)	0.31ms
WRN-28-10							
Baseline		4.06	19.54	36.45M (1.0×)	5.24B (1.0×)	2.52M (1.0×)	0.81ms
Recasting	Basic	**5.18**	**24.13**	1.46M (24.9×)	0.21B (24.5×)	0.52M (4.9×)	0.56ms
KD	Basic	5.48	25.28	1.46M (24.9×)	0.21B (24.5×)	0.52M (4.9×)	0.56ms
Backprop	Basic	5.39	25.78	1.46M (24.9×)	0.21B (24.5×)	0.52M (4.9×)	0.56ms

Table 5: Comparison of error rate (%) with previous works on ILSVRC2012. (B/M: billion/million)

Method	Top1	Top5	Params	Mults	Acts/batch	Actual speed-up
ResNet-50						
Recasting(C+R_{bt})	**25.00**	**7.71**	21.72M	2.40B	236.16M	**2.1×**
ThiNet-30 (Luo, Wu, and Lin 2017)	31.58	11.7	8.66M	1.10B	-	1.3×
AutoPruner ($r = 0.3$) (Luo and Wu 2018)	27.47	8.89	-	1.32B	-	-
VGG-16						
Recasting(C_A)	**30.05**	**10.38**	120.61M	3.12B	220.61M	**3.2×**
ThiNet-Conv (Luo, Wu, and Lin 2017)	30.20	10.47	131.44M	4.79B	-	2.5×
RNP (3×) (Lin et al. 2017)	-	12.42	-	-	-	2.3×
Channel Pruning (3×) (He, Zhang, and Sun 2017)	-	11.10	-	-	-	2.5×
AutoPruner ($r = 0.4$) (Luo and Wu 2018)	31.57	11.57	-	4.09B	-	-

Relational Knowledge Distillation

2019
CVPR

Relational Knowledge Distillation. In *CVPR*, 2019.

– Wonpyo Park, Dongju Kim, Yan Lu and Minsu Cho.

<Difference between KD and RKD>

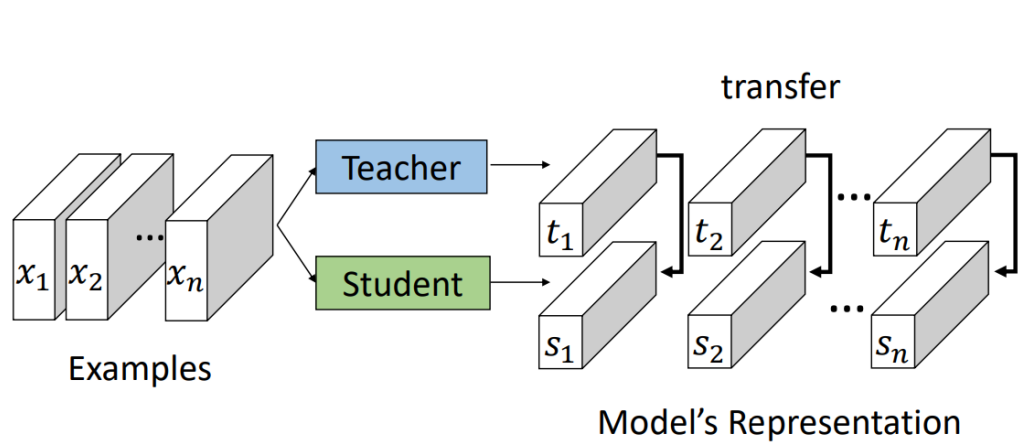# Relational Knowledge Distillation. In *CVPR*, 2019.

– Wonpyo Park, Dongju Kim, Yan Lu and Minsu Cho.

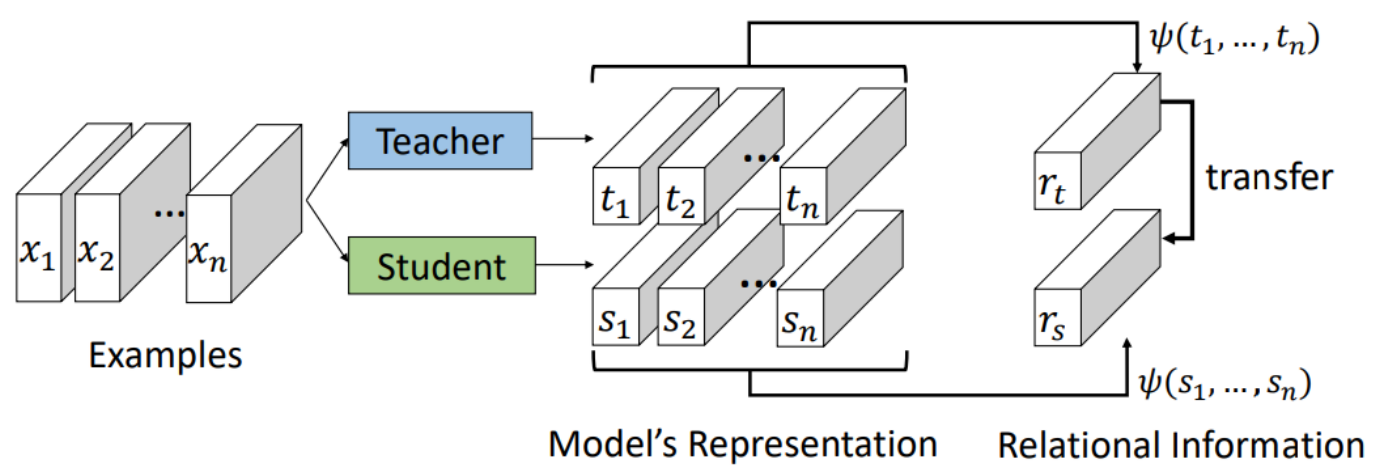**Individual Knowledge Distillation**

Relational Knowledge Distillation

$$\psi_{\mathrm{D}}(t_i, t_j) = \frac{1}{\mu} \|t_i - t_j\|_2$$

$$\mu = \frac{1}{|\mathcal{X}^2|} \sum_{(x_i, x_j) \in \mathcal{X}^2} \|t_i - t_j\|_2$$

$$\mathcal{L}_{\mathrm{RKD\text{-}D}} = \sum_{(x_i, x_j) \in \mathcal{X}^2} l_\delta\big(\psi_{\mathrm{D}}(t_i, t_j), \psi_{\mathrm{D}}(s_i, s_j)\big)$$

<Distance-wise distillation loss>

$$\psi_{\mathrm{A}}(t_i, t_j, t_k) = \cos \angle t_i t_j t_k = \langle \mathbf{e}^{ij}, \mathbf{e}^{kj} \rangle$$

$$\text{where} \quad \mathbf{e}^{ij} = \frac{t_i - t_j}{\|t_i - t_j\|_2}, \mathbf{e}^{kj} = \frac{t_k - t_j}{\|t_k - t_j\|_2}$$

$$l_\delta(x, y) = \begin{cases} \frac{1}{2}(x - y)^2 & \text{for } |x - y| \le 1 \\ |x - y| - \frac{1}{2}, & \text{otherwise.} \end{cases}$$

$$\mathcal{L}_{\mathrm{RKD\text{-}A}} = \sum_{(x_i, x_j, x_k) \in \mathcal{X}^3} l_\delta\big(\psi_{\mathrm{A}}(t_i, t_j, t_k), \psi_{\mathrm{A}}(s_i, s_j, s_k)\big)$$

<Angle-wise distillation loss>

Relational Knowledge Distillation. In *CVPR*, 2019.

– Wonpyo Park, Dongju Kim, Yan Lu and Minsu Cho.

Table 4: Accuracy (%) on CIFAR-100 and Tiny ImageNet.

	CIFAR-100 [15]	Tiny ImageNet [46]
Baseline	71.26	54.45
RKD-D	72.27	54.97
RKD-DA	72.97	56.36
HKD [11]	74.26	57.65
HKD+RKD-DA	**74.66**	**58.15**
FitNet [27]	70.81	55.59
FitNet+RKD-DA	72.98	55.54
Attention [47]	72.68	55.51
Attention+RKD-DA	73.53	56.55
Teacher	77.76	61.55

SUMMARY

- Regularizer

- Teaching & Learning

- Various Fields
  (Model Compression, Transfer Learning, Few shot Learning, Meta Learning…)

Q&A